**RESQUE: Network reduction using semi-Markov random walk scores for efficient querying of biological networks**

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**ABSTRACT**

Motivation: Recent technological advances in measuring molecular interactions have resulted in an increasing number of large-scale biological networks. Translation of these enormous network data into meaningful biological insights requires efficient computational techniques that can unearth the biological information that is encoded in the networks. One such example is network querying, which aims to identify similar subnetwork regions in a large target network that are similar to a given query network. Network querying tools can be used to identify novel biological pathways that are homologous to known pathways, thereby enabling knowledge transfer across different organisms.

Results: In this article, we introduce an efficient algorithm for querying large-scale biological networks, called RESQUE. The proposed algorithm adopts a semi-Markov random walk (SMRW) model to probabilistically estimate the correspondence scores between nodes that belong to different networks. The target network is iteratively reduced based on the estimated correspondence scores, which are also iteratively re-estimated to improve accuracy until the best matching subnetwork emerges. We demonstrate that the proposed network querying scheme is computationally efficient, can handle any network query with an arbitrary topology and yields accurate querying results.

Availability: The source code of RESQUE is freely available at http://www.ece.tamu.edu/~bjyoon/RESQUE/

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Supplementary Information: Supplementary data are available at Bioinformatics online.

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**1 INTRODUCTION**

Biological functions in cells are carried out through complicated interactions among various cellular constituents. For instance, protein-protein interactions (PPI) lie at the core of various transcriptional, signaling and metabolic processes in cells (Zhang et al., 2009). Quantitative genome-scale description of such interactions among various cellular constituents is encoded in the networks. One such example is network querying, which aims to identify similar subnetwork regions in a large target network that are similar to a given query network. Network querying tools can be used to identify novel biological pathways that are homologous to known pathways, thereby enabling knowledge transfer across different organisms.

**RESULTS:**

In this article, we introduce an efficient algorithm for querying large-scale biological networks, called RESQUE. The proposed algorithm adopts a semi-Markov random walk (SMRW) model to probabilistically estimate the correspondence scores between nodes that belong to different networks. The target network is iteratively reduced based on the estimated correspondence scores, which are also iteratively re-estimated to improve accuracy until the best matching subnetwork emerges. We demonstrate that the proposed network querying scheme is computationally efficient, can handle any network query with an arbitrary topology and yields accurate querying results.

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dynamic programming for network querying. Yang and Sze (2007) proposed two algorithms called PathMatch, which searches for the longest weighted path, and GraphMatch, which enumerates all possible solutions to find the highest scoring subgraphs in a directed acyclic graph. Qian et al. (2009) proposed a hidden Markov model (HMM)-based scheme for querying linear paths. SIGMA (Mongiovì et al., 2010) and RINQ (Gulsoy and Kahveci, 2011) consider the problem of efficient querying in biological network databases using indexing schemes. Ferraro et al. (2010) proposed an asymmetric approach that uses a master-slave scheme to extract, via the Viterbi algorithm, matching subgraphs in the master network. Another recent algorithm, called Torque (Bruckner et al., 2010), proposed a topology-free querying scheme that looks for a connected set of matching proteins in the target network that are sequence-similar to proteins in the query network, where the underlying motivation for taking a topology-free approach was the incompleteness of the currently available protein interaction data. Another algorithm called GraMoFoNe (Blin et al., 2010) adapted this topology-free approach, based on a color-coded motif matching scheme.

Currently, most network querying algorithms cannot handle queries with general network structures. Many algorithms either restrict the queries to have a relatively simple structure (e.g., linear path or tree) (Blin et al., 2010a; Castelli et al., 2008; Kelley et al., 2010a; Quint et al., 2009; Shlomi et al., 2008) or simply view it as a collection of nodes by ignoring the underlying topology (Blin et al., 2010a; Bruckner et al., 2010). Furthermore, many algorithms strongly rely on sequence similarity to identify homologous node pairs, where candidate pairs are typically identified by thresholding the similarity scores (e.g., BLAST score) (Blin et al., 2010a; Bruckner et al., 2010; Ferraro et al., 2010; Kelley et al., 2004). Besides, many network querying algorithms still suffer from high computational cost, which often increases exponentially with the query size, rendering them impractical for large queries (Fionda and Palopoli, 2011).

In this article, we propose a novel network querying algorithm, called RESQUE (REaction-based scheme using Semi-Markov scores for network querying) that can effectively address the shortcomings of existing algorithms. For fast and accurate network querying, the proposed algorithm takes an efficient reduction-based approach, where the target network is iteratively reduced based on the so-called node correspondence scores that are computed using a semi-Markov random walk (SMRW) model. The node correspondence score provides a probabilistic similarity measure between nodes that belong to different networks (i.e. query and target networks), which can be efficiently computed using a closed-form formula. At each iteration, the estimated scores are used to remove the nodes in the target network that have minimal correspondence to the nodes in the query network, thereby shrinking the search space. The node correspondence scores are then reestimated based on the reduced network and the aforementioned reduction process is repeated until the best matching subnetwork emerges. Based on real as well as synthetic examples, we demonstrate that RESQUE outperforms state-of-the-art network querying techniques, in terms of both computational efficiency and querying accuracy.

2 MATERIALS AND METHODS

Suppose we have a target PPI network, represented by an undirected weighted graph $G = (V, E, w)$, where $V$ is the set of $N$ nodes that correspond to the proteins in the network, $E$ is the set of $M$ edges that represent the protein interactions and $w$ is a weight function $w: E \rightarrow R$, representing the strength or reliability of an interaction. Let $G'_Q = (V'_Q, E'_Q, w'_Q)$ be the query network with a set $V'_Q$ of $N_Q$ nodes, edge set $E'_Q$ and interaction reliability $w'_Q$. In case the interaction reliability data are unavailable, we may simply assign uniform reliability score to all edges. For a pair of proteins $qv, v$, where $q_v \in V'_Q$ and $v \in V$, the node similarity is denoted as $h(qv, v)$. Typically, sequence similarity scores are used to measure this node similarity, although we may also use other measures based on structural or functional similarity between the proteins. The overall goal of network querying is to identify the subnetwork in the target network $G$ that is maximally similar to the given query network $G'_Q$.

2.1 Estimation of probabilistic node correspondence scores through SMRW

The network querying problem can be viewed as a mapping problem, in which we assign each query node $q_v \in V'_Q$ to one or more target nodes $v \in V$, based on their overall biological similarity. This biological similarity should be measured by integrating the node similarity between the matching proteins themselves as well as the similarity between their interaction patterns with other neighboring proteins. SMRW model can provide an effective means of obtaining such integrated similarity scores (Sahraeian and Yoon, 2011a,b). Markov random walk is a process that takes successive random steps (on a graph or a path) according to the Markov assumption. In an ordinary Markov random walk, the random walker always spends a fixed amount of time at a given position before making the next move. On the other hand, in a SMRW, the walker may spend a random amount of time between each transition. Herein, we consider a ‘simultaneous’ SMRW on both query and target networks, as shown in Figure 1. The position of the walker is updated every time at a given position before making the next move. On the other hand, in a SMRW, the walker may spend a random amount of time between each transition. Herein, we consider a ‘simultaneous’ SMRW on both query and target networks, as shown in Figure 2. The position of the walker is updated every time at a given position before making the next move. On the other hand, in a SMRW, the walker may spend a random amount of time between each transition. Herein, we consider a ‘simultaneous’ SMRW on both query and target networks, as shown in Figure 2. The position of the walker is updated every time at a given position before making the next move.
interaction reliability \( w(i, j) \) as follows:
\[
\alpha(i, j) = \frac{w(i, j)}{\sum_{k \neq j} w(i, k)}
\]
where \( N(i) \) is the set of neighbors of node \( i \). The transition probability \( \alpha(i, j) \) is also defined in a similar way.

We model the SMRW on \( \mathcal{G}_Q \) such that \( \mu(x) \), the expected amount of time that the random walker spends at a node pair \( x = (i, j) \), is proportional to the node similarity \( h_{QQ}(i, j) \). Using this model, we can measure the "global correspondence score" between \( q_i \) and \( q_j \) based on the long-run proportion of time that the random walker stays at the node pair \( x = (i, j) \). According to this model, both higher interaction similarity as well as higher node similarity will increase the long-run proportion of time that the random walker stays simultaneously at \( q_i \) and \( q_j \), making it a good measure for assessing the global similarity between nodes in different networks. As shown in Subramanian and Wong (2008), the global correspondence score described above can be computed as follows:
\[
\alpha(i, j) = \frac{\pi_x(i) \pi_x(j) \mu(x)}{\sum_{k \neq j} \pi_x(k) \mu(x)}
\]
where \( \pi_x \) is the steady-state distribution of the Markov random walk on \( \mathcal{G}_Q \), whose transition probability matrix is \( \mathcal{A}_Q \). According to a property of the product graph (Kamthe et al. 2010), we have \( \mathcal{A}_Q = \mathcal{A}_Q \otimes \mathcal{A}_Q \), where \( \mathcal{A}_Q \) and \( \mathcal{A}_Q \) are the steady-state distributions of the random walks on \( \mathcal{G}_Q \) and \( \mathcal{G}_Q \), respectively. We can compute the distributions \( \pi_x \) and \( \pi_y \) by, respectively, finding the eigenvectors of the transition matrices \( \mathcal{A}_Q \) and \( \mathcal{A}_Q \) with unit eigenvalue. For graphs that consist of multiple disconnected subgraphs, we find the steady-state distributions for each connected subgraph separately. Besides, we also add a self-transition edge to every isolated node in \( \mathcal{G}_Q \) and \( \mathcal{G}_Q \). We can conveniently rewrite \( \mathcal{A}_Q \) as
\[
\mathcal{A}_Q = \mathcal{P}_Q \mathcal{H} \mathcal{P}_Q^T \mathcal{H}^T
\]
where \( \mathcal{S}, \mathcal{H}, \) and \( \mathcal{P}_Q \) are \( \mathcal{N}_Q \times N \)-dimensional matrices such that \( S(l, j) = \pi_x(i(j)) \), \( H(l, j) = \pi_y(i(l)) \) and \( P(l, j) = \pi_x(i(l)) \pi_y(j) \) and denotes the Hadamard (element-wise) product.

As we have discussed, the SMRW model provides us with a computationally efficient method for computing probabilistic node correspondence scores that sensibly integrate node similarities and topological similarities. The estimated scores are used for iterative network reduction, which will be described in the next subsection. It is worth noting that a simple random walk-based scheme was recently proposed by Singh et al. (2006) in the context of global network alignment, which served as the basis of two popular network alignment algorithms called IsoRank (Singh et al. 2008) and IsoRankN (Liao et al. 2009). In this approach, the similarity between nodes in two different PPI networks is measured by solving a matrix equation, where the resulting similarity scores can be viewed as the stationary probabilities of a random walk with restart on the product graph. The transitions in this random walk are governed by the transition probability matrix \( \mathcal{A}_Q \), while the restart probability is governed by the node similarity score matrix \( \mathcal{H} \). One practical limitation of this scheme is the high computational complexity for computing the stationary probabilities, which requires us to find the eigenvector of a huge \( N \times N \)-dimensional square matrix, where \( N \) is the number of nodes in the product graph \( \mathcal{G}_Q \). On the other hand, the SMRW scheme decouples the problem of finding stationary probabilities of the random walk on the product graph \( \mathcal{G}_Q \) into two subproblems, each of which requires the computation of the stationary probabilities of the random walk on a single graph, as shown in \( \mathcal{A}_Q \) and \( \mathcal{H} \). This remarkably reduces the overall cost for computing the global node correspondence scores. For instance, for a query complex with \( N_Q \) nodes and \( m_Q \) edges, and the target network with \( N \) nodes and \( m \) edges, the time complexity of the random walk scheme proposed in Singh et al. (2006) is \( O(m + m_Q + 2) \), while that of the proposed SMRW scheme is \( O(m + m_Q + 2) \), with \( z \) the number of non-zero elements in \( \mathcal{H} \) (which corresponds to the number of potential homologues across the two networks). \( \mathcal{H} \) is a \( \mathcal{N}_Q \times N \) matrix, but in practice, it is highly sparse, hence \( z \ll N \mathcal{N}_Q \). The difference between the two schemes, in terms of complexity, will become more prominent for larger networks.

### 2.2 Iterative network reduction

To search for the best matching subnetwork region in the target network, we take a reduction-based approach, in which we shrink the search space through iterative network reduction. In this scheme, we repeatedly reduce the size of the target network by discarding the nodes with the lowest affinity to the query nodes, which is reflected in the global node correspondence scores measured by the SMRW model. In each iteration, we update the correspondence scores based on the reduced target network to re-estimate the affinity between nodes across the two networks. The main motivation underlying this iterative 'reduction and re-estimation' technique is that the estimated node correspondence scores in the \( \mathcal{H} \) matrix tend to be less reliable when there exist a large number of irrelevant nodes in the target network.

To tackle this problem, we iteratively filter out the least relevant nodes in the target network and re-estimate the correspondence scores so that the reliability of the estimated scores is successively refined through the iterations. In general, the proposed technique improves the reliability of the estimated node correspondence scores and leads to more accurate querying results, as will be discussed in this subsection and also demonstrated based on actual querying experiments in Section 3.

Before performing the iterative network reduction, we discard any potential non-homologous nodes from the target network, such that \( v_j \) \( \notin \mathcal{V}_T \) and all its edges are removed if \( v_j \in \mathcal{V}_Q \). This pruning step can reduce false-positive errors and improve the overall speed of the querying algorithm. At the beginning of the reduction process, we let \( \mathcal{G}_Q^0 = \mathcal{G}_T \) to be the initial network. Then, in the \( k \)th iteration, we update \( \mu^{k+1}(l, j) = \mu^k(l, j) \mathcal{G}_T^k(l, j) \) to \( \mathcal{G}_Q^{k+1} = \mathcal{G}_T^{k+1} \) based on the network \( \mathcal{G}_Q^k \). Next, we select the node \( v_j \) \( \in \mathcal{V}_Q^k \) with the lowest correspondence score to the query network as described in the following. Let \( a^*(l, j) \) be the (unknown) optimal mapping between the query network \( \mathcal{G}_Q^k \) and the best-matching subnetwork in the target \( \mathcal{G}_T \). We define the minimal correspondence node \( \nu_j \) as
\[
d = \arg\min_{j \in \mathcal{V}_Q^k} \mu(l, j) = \arg\min_{j \in \mathcal{V}_Q^k} \mathcal{P}_Q^T \mathcal{H} \mathcal{P}_Q \mu(l, j)
\]
where we view the correspondence score \( \mathcal{S}^Q(l, j) \) (estimated in the current iteration \( k \)) as an estimator of \( \mathcal{P}_Q(l, j) \), which is the posterior probability that the query node \( q_l \) is mapped to the target node \( v_j \) in the optimal mapping \( a^* \). According to \( \mathcal{B}_Q \), \( \nu_j \) will be the node that is least likely to be included in the best matching subnetwork region. Thus, we discard \( \nu_j \) and its edges from \( \mathcal{G}_Q^{k+1} \) to obtain \( \mathcal{G}_Q^{k+1} \). Unless \( \nu_j \) is the only homologous node (in the current target network) for some query node \( q_l \). More precisely, if there exists a \( q_l \) \( \in \mathcal{V}_Q^k \) such that \( \mathcal{S}^Q(l, j) = 0 \) and \( \mathcal{S}^Q(l, j) > 0 \) for all \( j \neq \nu_j \) in the network and check the next candidate node. This reduces the risk of discarding a true match with a relatively low correspondence score. After the node removal at each iteration, we also discard all isolated nodes \( \mathcal{V}_Q^k \setminus \{v_j, \nu_j \} \), unless the isolated node is the only homologous node of a query node. The set \( \mathcal{V}_Q^k \) can be easily identified, as it simply consists of nodes in \( \mathcal{V}_Q^k \) whose only neighbor is \( \nu_j \). Following this reduction step, we recompute the correspondence scores \( \mathcal{S}^Q \) based on the reduced network, to be used in the next iteration. We repeat the network reduction and score re-estimation process until we have
After the network reduction process, we are left with a reduced target network. Therefore, the maximum weighted matching on the bipartite graph with edge weight bipartite matching (MWM) problem. For each query node \( f \), we denote its (unknown) true matching node in the target network as \( v_j \). Through this, the indicator function whose value is 1 if the argument is true, and 0 otherwise. In practice, the true mapping \( a^* \) is unknown. Instead, after assessing the accuracy defined in (3), we estimate the ‘expected accuracy’ as follows:

\[
E_{w}(\text{accuracy}(a^*, a)) = \frac{1}{N_Q} \sum_{q_i} E_{w}(H[q_i \sim v_j \sim a^*]),
\]

where \( P(q_i \sim v_j \sim a^*) \) is the posterior probability of that \( q_i \) will be mapped to \( v_j \) in the true mapping \( a^* \). Based on this setting, the goal of network querying would be to find the optimal mapping \( a \in \mathcal{A} \) that has the maximum expected accuracy. Note that the concept of maximum expected accuracy was previously adopted by a number of multiple sequence alignment algorithms. Here, we seek the maximum expected accuracy querying result. As discussed in the previous section, this can be found by maximizing the objective function \( f(S) = \sum_{q_i} S_i \cdot (r_i) \). As mentioned earlier, this corresponds to finding the maximum weighted matching \( M \) on the bipartite graph \( G \). Otherwise, in the case of the topological approach, in which it searches for a connected set of nodes \( K \) in the reduced target network \( G^R \) and report this network \( G_t \) as the final querying result. Since all remaining nodes in the reduced network \( G^R \) have high correspondence to the query nodes, \( G_t \) is guaranteed to be highly similar to the query network \( G_q \). We refer to this second network querying scheme as RESQUE-C (for largest Connected component). In case the target network contains two duplicated copies of the proteins across PPI networks, both copies will be present in the reduced target network \( G^R \) at the end of the iterative reduction process, with high probability. RESQUE-C will return both copies in the final result, assuming they are connected. On the other hand, RESQUE-M will generally report only one of the nodes with a higher correspondence score, for each pair of duplicated nodes.

2.4 Materials
We assess the performance of RESQUE based on the PPI networks of *Drosophila melanogaster*, *Homo sapiens*, and *Saccharomyces cerevisiae*, which are the three largest PPI networks that are currently available. We obtained the PPI data from IsoBase [6, 7], a recently published database of functionally related proteins across PPI networks. IsoBase consists of several PPI networks that belong to different species, along with the homology scores between all pairs of proteins across species (measured in terms of the BLAST bit-value similarity between the protein sequences). The PPI networks in IsoBase have been constructed by integrating the PPI data from three different public databases: DIP [8], BioGRID [9], and HPRD [10]. Currently, the D. melanogaster PPI network in IsoBase contains 41508 proteins and 26726 interactions, the *H. sapiens* network contains 23369 proteins and 43757 interactions, and the *S. cerevisiae* network includes 6659 proteins and 38109 interactions. The query networks were obtained by taking protein complexes of size 4–25 in the D. melanogaster PPI network and projecting each complex to the corresponding PPI network to find its induced subnetwork.

3 Results
To investigate the performance of the proposed network querying algorithm, we conducted a set of querying experiments based on real PPI datasets as well as a number of simulated examples.

3.1 Querying performance on real PPI datasets
We first evaluated the performance of RESQUE by performing queries in the PPI networks of *D. melanogaster*, *H. sapiens*, and *S. cerevisiae*. We compared RESQUE against two state-of-the-art network querying algorithms: Torque [11] and IsoRankN [12]. Torque adopts a topology-free approach, in which it searches for a connected set of proteins (in the target network) that are homologous to the query proteins, without taking the topology of the query network into account. We chose to compare RESQUE with Torque, as...
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Results

Fig. 3. Performance of different querying algorithms. For each query/target pair, we report the number of MH, the number of functionally coherent hits (FC) and the number of specific hits (SP). (dme: \textit{D. melanogaster}, hsa: \textit{H. sapiens} and sce: \textit{S. cerevisiae}).

Fig. 2. Performance of different querying algorithms. For each query/target pair, we report the number of feasible hits (i.e. the total number of query complexes of size 4–25 that were used in our querying experiments), the number of hits and the number of MH, for all pairs of query and target species. As we see from this result, almost all hits returned by RESQUE-C and Torque are strongly connected, while IsoRankN and RESQUE-M yield a larger number of hits that are loosely connected. Figure 2 also shows that, on average, RESQUE-C can identify MH for 51% query complexes, while RESQUE-M returns MH for 39% complexes and both IsoRankN and Torque for 35% complexes. Also note that Torque typically has a smaller number of hits, as it can handle only a pre-specified number of indels (i.e. insertions/deletions).

To evaluate the accuracy of the querying algorithms, we measured the ‘functional coherence’ and ‘specificity’ of the querying results, as in Bruckner \textit{et al.} \cite{2010}. Functional coherence measures the relative number of hits with significant functional coherence, which is assessed based on the Gene Ontology (GO) \cite{2000} annotation. We used the GO TermFinder \cite{2004} to compute the false discovery rate (FDR) corrected $P$-value of the functional coherence of the proteins in the retrieved target subnetwork. The specificity is computed based on the relative number of hits that significantly overlap with a known protein complex. We used a similar statistical procedure as in Bruckner \textit{et al.} \cite{2010} to measure the significance of the overlap. Figure 3 shows the performance of the respective querying algorithms for different pairs of query and target species, in terms of the number of MH, the number of FC and the number of specific hits (SP). As we can observe, all four algorithms have similar levels of specificity (SP/MH > 0.8) and functional coherence (FC/MH > 0.9). However, the results clearly show that RESQUE-C yields the largest FC and SP. Considering the high functional coherence of the hits reported by RESQUE, the MH that do not overlap with known protein complexes may correspond to novel complexes. RESQUE-C and
Yoon (2011a), whose results can be found in the Supplementary Section S3. As we can observe, RESQUE is highly robust against changes in the node similarity scores. Furthermore, Figure 5 also shows that RESQUE is highly robust against changes in the node similarity scores. Additionally, Figure 6B illustrates the result of querying the Mitogen-activated protein kinase (MAPK) signaling pathway of the query network, we conducted further querying experiments based on simulated examples. In these experiments, we randomly extracted 100 connected subnetworks with general topology from the S. cerevisiae PPI network, where the size of each subnetwork ranged between 5 and 20. We applied two different types of perturbations to each query network. First, we considered a topological perturbation, where 7% of the query nodes were randomly deleted and inserted. Second, we perturbed the BLAST bit-value similarity scores by scaling the original similarity score by a random number drawn from a Gaussian distribution with mean \( \mu = 1 \) and variance \( \sigma^2 \).

Figure 4 shows the querying accuracy of different algorithms, for four different indel rates (\( \nu = 0, 10, 20 \) and 30%) and various sequence perturbation levels (\( \sigma \in [0.05, 0.5] \)). As we can observe, RESQUE is highly robust against changes in the node similarity scores. Furthermore, Figure 5 also shows that RESQUE is robust to topological changes that involve node deletions and insertions. The results clearly demonstrate the effectiveness of the SMRW model and the reduction-based approach in identifying the true matching nodes across networks. In all cases, RESQUE outperformed IsoRankN, in terms of both accuracy and robustness.

For comparison, we also performed similar experiments using Torque (results not shown). These experiments showed that Torque is almost invariant to changes in sequences similarity scores, which is expected as Torque uses the similarity score just to determine the presence (or absence) of homology between proteins. However, Torque typically showed lower accuracy compared with RESQUE and IsoRank, which was 88.8% for \( \nu = 0 \), 79.13% for \( \nu = 10 \), 72.26% for \( \nu = 20 \) and 60.75% for \( \nu = 30 \).

### 3.3 Querying performance on simulated data

In order to evaluate the robustness of the proposed network querying scheme to changes in the node similarity scores as well as the topology of the query network, we conducted further querying experiments based on simulated examples. We randomly extracted 100 connected subnetworks with general topology from the S. cerevisiae PPI network, where the size of each subnetwork ranged between 5 and 20. We applied two different types of perturbations to each query network. First, we considered a topological perturbation, where 7% of the query nodes were randomly deleted and inserted. Second, we perturbed the BLAST bit-value similarity scores by scaling the original similarity score by a random number drawn from a Gaussian distribution with mean \( \mu = 1 \) and variance \( \sigma^2 \).

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Fig. 6. Querying examples. (A) Querying the MAPK signaling pathway of *S. cerevisiae* in *H. sapiens*. Matching nodes are connected by dashed lines. (B) Querying the proteasome complex of *H. sapiens* in *S. cerevisiae*. (C) Querying the prefoldin complex of *S. cerevisiae* in *D. melanogaster*. (D) Querying the transcription factor TFIID complex of *D. melanogaster* in *S. cerevisiae*. (E) Querying the RNA polymerase complex of *S. cerevisiae* in *H. sapiens*.

Kanehisa and Goto (2000) in the PPI network of *H. sapiens*. The querying result is in good agreement with the MAPK signaling pathway of *H. sapiens*, and the identified subnetwork shows high functional coherence (P-value of $1.91 \times 10^{-11}$), measured based on GO annotations. The next example in Figure 6B represents the result of querying the proteasome complex of *H. sapiens* in the *S. cerevisiae* PPI network. The querying result closely matches the proteasome core complex in *S. cerevisiae* with high GO enrichment (P-value of $3.65 \times 10^{-42}$). The next three examples shown in Figures 6C–E are three instances where RESQUE could successfully predict the matching subnetwork, whereas Torque was not able to find a hit for the given query. Figure 6C illustrates the result of querying the prefoldin complex of *S. cerevisiae* in the *D. melanogaster* PPI network. The matching proteins reported by RESQUE belong to the same complex in *D. melanogaster* with high GO enrichment (P-value of $2.87 \times 10^{-15}$). Next, Figure 6D shows the querying result of the transcription factor TFIID complex of *D. melanogaster* in the *S. cerevisiae* PPI network. RESQUE was able to identify the matching TFIID proteins with high GO enrichment with a P-value of $1.41 \times 10^{-15}$. Finally, Figure 6E illustrates the result of querying the RNA polymerase complex of *S. cerevisiae* in the PPI network of *H. sapiens*, where the retrieved subnetwork closely matched the query network and contained proteins that are functionally coherent (P-value of $8.30 \times 10^{-29}$). These examples clearly show that RESQUE can efficiently search biological networks based on queries that have general topology, effectively handle node insertions and deletions and yield biologically significant results. In Supplementary Tables S1–S6 we also report a list of novel querying results obtained by RESQUE-C for queries for which IsoRankN and Torque failed to identify MH.

4 CONCLUSION

In this article, we proposed RESQUE, a novel network querying algorithm that can efficiently query biological pathways and molecular complexes in large-scale biological networks. The algorithm uses a SMRW model to estimate probabilistic correspondence scores between nodes across different networks, which are used to identify the best match to the given query according to the maximum expected accuracy principle. RESQUE adopts an iterative network reduction and score re-estimation technique to improve the expected accuracy of the final querying result. As discussed in this article, RESQUE does not restrict the topology of the query network, and it can handle paths, trees and loopy graphs. The algorithm supports both connected and partially connected query networks. In the extreme case, RESQUE can also be used with a query pathway (or complex) with an unknown topology, in which case we can simply treat the query as a collection of isolated nodes. In this case, the steady-state distribution of the random walk on the query network, $\pi_Q$, will be uniform over all the query nodes. Furthermore, RESQUE can effectively deal with node insertions and deletions at arbitrary locations. Despite its generality, RESQUE has very low computational complexity, which allows us to use the algorithm for querying large pathways/complexes in genome-scale networks. Experimental results based on real and synthetic examples...
show that RESQUE outperforms other popular algorithms, in terms of speed, accuracy and robustness.

Although we have not explored the application of RESQUE to directed networks, it is worth noting that such extension would be relatively straightforward. In fact, in order to incorporate the edge directions when estimating the node correspondence scores, we only have to require the SMRW to follow these directions during the random walk (i.e. by choosing the next node among the neighbors that are connected through outgoing edges).

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