treePL: divergence time estimation using penalized likelihood for large phylogenies

Stephen A. Smith¹,* and Brian C. O'Meara²

¹Department of Ecology and Evolutionary Biology, University of Michigan, Ann Arbor, MI, 48109 and ²Department of Ecology and Evolutionary Biology, University of Tennessee, Knoxville, TN, 37996 USA

1 INTRODUCTION

Divergence times make phylogenetic hypotheses easier to interpret in light of other information on geology, biogeography and co-diversification. A number of methods exist for transforming branch lengths to be proportional to time. However, many of these methods do not scale well for phylogenies with thousands of taxa. The number of species included in published phylogenies has exploded (Goloboff et al., 2009; Smith et al., 2009). With the increase in the size of phylogenies, there is the need to develop divergence time methods that are capable of handling larger datasets. Here, we present a method, implemented in the software treePL, for calculating divergence time estimates using penalized likelihood that can handle datasets of thousands of taxa. We implement a method that combines the standard derivative-based optimization with a stochastic simulated annealing approach to overcome optimization challenges. We compare this approach with existing software including r8s, PATHd8 and BEAST.

2 METHODS

2.1 Penalized likelihood

The optimality criterion used in this article is the penalized likelihood framework described in Sanderson (2002). Note that though this is framed as a likelihood method, it is possible to interpret this as a maximum a posteriori estimate in a Bayesian context given particular priors (Thorne and Kishino, 2005). It is also possible, following Sanderson’s modifications to r8s, to use a related penalty that uses the differences of log rates rather than differences of untransformed rates (the additive penalty). This has been implemented in treePL, but analyses below use the original additive penalty.

2.2 The algorithm

Divergence time estimation, and penalized likelihood especially, presents a number of optimization challenges. One challenge is the large number of parameters and the ratio of free parameters to observations. This can be dampened by a large penalty function, but still presents a parametric optimization problem. The second challenge is the presence of barriers placed by both the user and the hierarchical nature of phylogenies. We present a first step to overcoming these problems with extremely large phylogenies. Our algorithm includes two main phases: a greedy hill-climbing phase and a stochastic phase. This combination is meant to both speed optimization and avoid local optima.

The greedy phase of the optimization step consists of two gradient-based optimization rounds. The first round of optimization uses gradient values from an exact gradient calculator with math derived from Sanderson (2002). The second round of optimization uses auto-differentiation (Gay, 2005; Griewank et al., 1996). Auto-differentiation, because it has the same complexity as the original function, often continues hill climbing after the exact gradient calculator fails. However, we have found, empirically, that alone it is not as efficient and requires more rounds and restarts than combining exact gradients and auto-differentiation.

We found that a stochastic phase, in this case a partial simulated annealing procedure, is helpful in easing the parameters away from local optima. We consider it partial as the step does not consist of a full simulated annealing run. Instead, the phase consists of thousands of stochastic optimization generations followed by intermittent greedy phases. Although this additional step may lengthen convergence time, the result will often improve.

The performance of optimization methods can vary dramatically by dataset. We have provided a ‘priming’ step that will run through each optimization option and report those that show the greatest difference in starting and stopping likelihood scores. Although this can help, researchers should replicate analyses and experiment with settings to assure convergence. We have also provided a ‘wiggle’ option that will report divergence times that are within two log likelihood units of the best likelihood, suggested by Edwards (1992) as a confidence window. This allows for the visualization of nodes that are particularly uncertain, but...
does not account for all sources of uncertainty (e.g. calibration uncertainty or branch length errors).

2.2.1 Cross-validation The penalized likelihood approach requires the identification of a smoothing parameter that affects the penalty for rate variation over the tree. A cross-validation procedure is used to determine the best smoothing parameter. We provide two options for cross-validation: leave one out cross-validation (LOOCV) and random subsample and replicate cross-validation (RSRCV). The LOOCV approach is described in Sanderson (2002) and requires iteratively removing each terminal node, recalculating rates and dates, and recording the error between the predicted value from the estimate and the observed value. RSRCV randomly samples, with replacement, multiple terminal nodes, recalculates rates and dates with these terminal nodes removed and calculates the average error over the sampled nodes. RSRCV replicates this procedure a number of times, with 10 times being typical. Potential sets of terminal nodes that cause the removal of internal nodes (such as a set of terminal nodes that form a clade) are not allowed. This procedure is much faster than LOOCV and produces similar results. Cross-validation can be unstable, but subsampling procedures such as RSRCV may improve this behavior (Kohavi, 1995).

2.2.2 Implementation The above algorithm is implemented in treePL, which is open source and available at https://github.com/blackrim/treePL. Auto-differentiation uses RAD (Gay, 2005; Griewank et al., 1996) on a single core and ADOL-C for multiple cores. Likelihood calculations and cross-validation analyses may be distributed on multicore machines using the OpenMP library.

3 SIMULATIONS

We test the performance of treePL, r8s and PATHd8 (Britton et al., 2007) on simulated datasets with up to 10000 taxa. Two empirical examples, including comparisons to BEAST, may be seen in the Supplementary Materials, as can details of the simulations.

To measure the performance of each method, we measured the $R^2$ of the estimated node ages against the known node ages (Fig. 1). r8s and treePL perform quite similarly and both perform better than PATHd8. Some of the slight performance decrease of treePL as tree size increases may be explained by numerical error with treePL adding nonzero values to effectively zero branch lengths. The poor performance of PATHd8 for many of these trees may be a result of how it resolves conflicting dates and rates. In these cases, PATHd8 allows the conflicting branches to have the same height, thus sinking the branch to its parent, leading to a zero branch length.

The time it took to run each analysis was also recorded (Fig. 1 inset). PATHd8 analyses are almost instantaneous. treePL is far faster than r8s but slower than PATHd8. Nevertheless, r8s performs well for smaller datasets. The runtime for treePL is highly dependent on the nature of the dataset, the settings for the stochastic phase of the run, and the optimization method used for the greedy phase. Parallelization in treePL was not used for the simulation runs.

The simulated analyses demonstrate that, at least under the particular settings of the simulator, r8s and treePL perform well with treePL being significantly faster than r8s (see Supplementary Materials for performance with empirical datasets). Both programs perform better than PATHd8 in terms of accuracy when compared with the ‘true’ simulated tree. The simulated analyses also demonstrate that divergence-time analysis with penalized likelihood is reasonable on trees of over 10000 taxa.

Fig. 1. The performance of r8s, treePL and PATHd8 on the simulated datasets as measured by $R^2$ of estimated node ages against known ages. The inset shows average runtimes of r8s, treePL and PATHd8 in minutes on simulated datasets. Error bars represent 95% confidence intervals

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REFERENCES


