## Supplementary documents for "Cell-level somatic mutation detection from single-cell RNA-sequencing" <br> By Trung Nghia Vu, et al

## Details of 2D local false discovery rate estimation

Here we describe in detail the estimation of 2D local false discovery rate (fdr2d) in the context of mutation detection from scRNA-seq data. For completeness and clarity, some parts from the main text are repeated.

Denote by $\mathrm{SNV}_{1}, \ldots, \mathrm{SNV}_{m}$ the bc-mutation sites from the bcDNA-seq data. The observed statistics are $z$ values from these $m$ SNVs across all single cells $1, \ldots, n$. Let $\mathbf{Z}$ be the $m \times n$ matrix of observed $z$ values. For convenience, assume each cell of the matrix contains the pair of statistics $\left(z_{1}, z_{2}\right)$. The data required to estimate $f_{0}(z)$ are based on $K$ random samples, each of size $m$, of the null SNVs, i.e. the non bc-mutation sites. As for the bc-mutations we limit to SNVs with VAF $=0$ in the germline, since somatic mutations are not likely to have any variant in germline. Denote these samples as $\mathbf{Z}_{1}^{*}, \ldots, \mathbf{Z}_{K}^{*}$, representing samples of $\mathbf{Z}$ under the null hypothesis of no mutation.

The procedure first estimates a 2D function

$$
r(z) \equiv \frac{K f_{0}(z)}{f(z)+K f_{0}(z)},
$$

and then computes the fdr2d as

$$
\begin{equation*}
\operatorname{fdr} 2 \mathrm{~d}(z)=\pi_{0} \frac{r(z)}{K\{1-r(z)\}}, \tag{1}
\end{equation*}
$$

The 2d-estimation of $r(z)$ involves:

1. treating all the statistics from $\mathbf{Z}_{1}^{*}, \ldots, \mathbf{Z}_{K}^{*}$ as 'successes' and the observed statistics from $\mathbf{Z}$ as 'failures', so that $r(z)$ is the proportion of successes as a function of $z$.
2. performing a nonparametric smoothing of the success-failure proportion as a function of $z$.

Because the full set of permuted data is large, to speed up computations, we pre-bin the data of the two dimensional grids, and the smoothing procedure to estimate the fdr2d is implemented on the grids. Since SNVs with small VAF $(<c)$ are not likely genuine mutations, the corresponding fdr2d values are set to 1 ; in practice we use the cutoff $c=0.2$.

From hereon the theory follows Pawitan (2001, Section 18.10). Let $y_{i j}$ be the number of successes in the $(i, j)$ location of the grid, and $N_{i j}$ the corresponding total number of points that fall in the $(i, j)$ location. By construction, $y_{i j}$ is binomial with size $N_{i j}$ and probability $r_{i j}$, the discretized version of $r(z)$. Given a smoothing parameter $\lambda$, the smoothed estimate of $r_{i j}$ is the minimizer of the penalized log-likelihood

$$
\log L(r, \lambda)=-\sum_{i j}\left\{y_{i j} \log r_{i j}+\left(N_{i j}-y_{i j}\right) \log \left(1-r_{i j}\right)\right\}+\lambda \sum_{(i, j) \sim(k, l)}\left(\eta_{i j}-\eta_{k l}\right)^{2}
$$

where $(i, j) \sim(k, l)$ means that $(i, j)$ and $(k, l)$ are primary neighbors in the 2D grids. The estimate is computed using the iteratively weighted least-squares (IWLS) algorithm, which
is a very stable algorithm in this case. Define the following arrays:

$$
\begin{aligned}
Y & \equiv \operatorname{vec}\left(y_{i j}\right) \\
r & \equiv \operatorname{vec}\left(r_{i j}\right) \\
\Sigma & \equiv \operatorname{Diag}\left[N_{i j} r_{i j}\left(1-r_{i j}\right)\right],
\end{aligned}
$$

and $R$ is the relationship matrix representing the primary neighbors (i.e. North, South, East and West) in the 2D grids. Let $k$ or $l$ be the 1D index of vector $Y$; the elements of $R^{-1} \equiv \operatorname{Diag}\left[e_{k l}\right]$ are given by

$$
\begin{aligned}
e_{k k} & =\text { number of primary neighbors of } k \\
e_{k l} & =-1 \text { if } l \text { is a primary neighbor of } k, \text { and } 0 \text { otherwise. }
\end{aligned}
$$

Starting with an initial estimate $r^{(0)}$ needed to compute the variance matrix $\Sigma$, the IWLS updating equation is

$$
r^{(1)}=\left(\Sigma^{-1}+\lambda R^{-1}\right)^{-1} \Sigma^{-1} Y .
$$

For speed, a fast inversion algorithm based on the Gauss-Seidel algorithm is used. At convergence, the output of the algorithm is a smooth estimate of $r(z)$, evaluated at discrete points $(i, j)$. The fdr2d is then computed using (1), then interpolated at each observed $z$. The amount of smoothing as a function of $\lambda$ is assessed by the effective number of degrees of freedom (df), computed using

$$
\mathrm{df}=\operatorname{trace}\left\{\left(\Sigma^{-1}+\lambda R^{-1}\right)^{-1} \Sigma^{-1}\right\} .
$$

In practice, we use a relatively coarse grid on the order of $25 \times 25$ points, and $\lambda$ is chosen so that df is approximately $70-80 \%$ of the number of grid points.

## References

Pawitan,Y. (2001) In All Likelihood: Statistical Modelling and Inference Using Likelihood. Oxford University Press.

## TABLES

Table S1: List of 99 confirmed-somatic mutations of the MDA-MB-231 cell-line from the COSMIC database

| Position_hg19 | Position_hg38 | ref | alt | contig | Gene |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16:2347421 | 16:2297420 | C | G | 16 | ABCA3 |
| 1:94502904 | 1:94037348 | G | A | 1 | ABCA4 |
| 4:175898171 | 4:174977020 | C | A | 4 | ADAM29 |
| 18:56191223 | 18:58523991 | G | A | 18 | ALPK2 |
| 1:145473530 | 1:145961557 | C | T | 1 | ANKRD34A |
| 1:197074117 | 1:197104987 | T | C | 1 | ASPM |
| 1:154315369 | 1:154342893 | C | T | 1 | ATP8B2 |
| 6:90661568 | 6:89951849 | G | T | 6 | BACH2 |
| 7:140481417 | 7:140781617 | G | T | 7 | BRAF |
| 10:124692048 | 10:122932532 | G | T | 10 | C10orf88 |
| 20:31690818 | 20:33103012 | G | C | 20 | C20orf186 |
| 9:139929258 | 9:137034806 | C | A | 9 | C9orf139 |
| 19:42383297 | 19:41879227 | G | A | 19 | CD79A |
| 7:143018844 | 7:143321751 | G | C | 7 | CLCN1 |
| 1:224553630 | 1:224365928 | T | C | 1 | CNIH4 |
| 13:111134863 | 13:110482516 | G | C | 13 | COL4A2 |
| 2:228145243 | 2:227280527 | G | T | 2 | COL4A3 |
| 15:91185244 | 15:90642012 | C | G | 15 | CRTC3 |
| 1:197611911 | 1:197642781 | A | G | 1 | DENND1B |
| 7:95709774 | 7:96080462 | C | A | 7 | DYNC1I1 |
| 2:27587647 | 2:27364780 | G | C | 2 | EIF2B4 |
| 3:89499345 | 3:89450195 | G | T | 3 | EPHA3 |
| 19:17873592 | 19:17762783 | G | A | 19 | FCHO1 |
| 10:93668048 | 10:91908291 | C | A | 10 | FGFBP3 |
| 16:90108924 | 16:90042516 | A | G | 16 | GAS8 |
| 1:35250656 | 1:34785055 | G | A | 1 | GJB3 |
| 16:27473769 | 16:27462448 | G | A | 16 | GTF3C1 |
| 4:2238074 | 4:2236347 | G | C | 4 | HAUS3 |
| 4:996138 | 4:1002350 | T | C | 4 | IDUA |
| 17:42463246 | 17:44385878 | C | G | 17 | ITGA2B |
| 10:7684028 | 10:7642065 | T | G | 10 | ITIH5_ENST00000397145 |
| 2:42671535 | 2:42444395 | G | A | 2 | KCNG3 |
| 19:51512761 | 19:51009505 | G | T | 19 | KLK9 |
| 6:63990177 | 6:63280272 | G | T | 6 | LGSN |
| 19:5699098 | 19:5699087 | G | A | 19 | LONP1 |
| 1:113655185 | 1:113112563 | A | G | 1 | LRIG2 |
| 12:40753186 | 12:40359384 | T | G | 12 | LRRK2 |
| 12:91502008 | 12:91108231 | C | G | 12 | LUM |
| X:30254741 | X:30236624 | G | A | X | MAGEB3 |
| X:135308130 | X:136225971 | C | T | X | MAP7D3 |
| 10:129902653 | 10:128104389 | T | C | 10 | MKI67 |


| 11:102662148 | 11:102791417 | C | G | 11 | MMP1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11:59828671 | 11:60061198 | C | A | 11 | MS4A3 |
| 5:80109433 | 5:80813614 | G | A | 5 | MSH3 |
| 8:15967689 | 8:16110180 | G | C | 8 | MSR1 |
| 8:121458742 | 8:120446502 | G | A | 8 | MTBP |
| 3:172365720 | 3:172647930 | G | A | 3 | NCEH1 |
| 22:30057209 | 22:29661220 | G | T | 22 | NF2 |
| 19:56321531 | 19:55810165 | G | C | 19 | NLRP11 |
| 19:15300174 | 19:15189363 | A | T | 19 | NOTCH3 |
| X:30327002 | X:30308885 | C | A | X | NR0B1 |
| 11:64402898 | 11:64635426 | G | T | 11 | NRXN2 |
| 1:114524167 | 1:113981545 | G | A | 1 | OLFML3 |
| 5:180166905 | 5:180739905 | G | T | 5 | OR2Y1 |
| 19:8841481 | 19:8731119 | G | T | 19 | OR2Z1 |
| 11:123810829 | 11:123940122 | G | C | 11 | OR4D5 |
| 11:4661717 | 11:4640487 | C | G | 11 | OR51D1 |
| 6:10702647 | 6:10702414 | G | T | 6 | PAK1IP1 |
| 10:55583094 | 10:53823334 | A | T | 10 | PCDH15 |
| 11:117100406 | 11:117229690 | C | G | 11 | PCSK7 |
| 4:55129981 | 4:54263814 | A | T | 4 | PDGFRA |
| 12:123481962 | 12:122997415 | G | A | 12 | PITPNM2 |
| 22:46652694 | 22:46256797 | G | T | 22 | PKDREJ |
| 22:46652691 | 22:46256794 | G | A | 22 | PKDREJ |
| 2:160885397 | 2:160028886 | G | C | 2 | PLA2R1 |
| 2:95943702 | 2:95277954 | C | T | 2 | PROM2 |
| 11:47444153 | 11:47422602 | G | T | 11 | PSMC3 |
| 11:47446725 | 11:47425174 | G | C | 11 | PSMC3 |
| 10:62645965 | 10:60886207 | G | T | 10 | RHOBTB1 |
| 6:4996598 | 6:4996364 | C | T | 6 | RPP40 |
| 19:39077183 | 19:38586543 | G | T | 19 | RYR1 |
| 5:54640988 | 5:55345160 | A | T | 5 | SKIV2L2 |
| 2:219249912 | 2:218385189 | T | A | 2 | SLC11A1 |
| 6:34730386 | 6:34762609 | G | C | 6 | SNRPC |
| 16:2814371 | 16:2764370 | C | T | 16 | SRRM2 |
| 6:36463589 | 6:36495812 | T | C | 6 | STK38 |
| 14:64593156 | 14:64126438 | C | A | 14 | SYNE2 |
| 6:149699796 | 6:149378660 | C | T | 6 | TAB2 |
| 16:89972658 | 16:89906250 | C | G | 16 | TCF25 |
| 20:61488922 | 20:62857570 | G | A | 20 | TCFL5 |
| 15:29997732 | 15:29705528 | G | T | 15 | TJP1 |
| 9:35706092 | 9:35706095 | A | T | 9 | TLN1 |
| 6:47251976 | 6:47284240 | C | T | 6 | TNFRSF21 |
| 17:7577099 | 17:7673781 | G | A | 17 | TP53 |
| 6:41121537 | 6:41153799 | C | A | 6 | TREML1 |
| 5:14502720 | 5:14502611 | A | G | 5 | TRIO |
| 5:14330953 | 5:14330844 | C | G | 5 | TRIO |


| $6: 41011373$ | $6: 41043634$ | C | A | 6 | TSPO2 |
| :--- | :--- | :--- | :--- | :---: | :--- |
| $20: 30510808$ | $20: 31923005$ | G | A | 20 | TTLL9 |
| $3: 48646621$ | $3: 48609188$ | G | T | 3 | UQCRC1 |
| $17: 48918070$ | $17: 50840709$ | A | T | 17 | WFIKKN2 |
| $12: 970240$ | $12: 861074$ | G | T | 12 | WNK1 |
| $2: 135744526$ | $2: 134986956$ | T | G | 2 | YSK4_ENST00000375845 |
| $14: 64989274$ | $14: 64522556$ | A | T | 14 | ZBTB1 |
| $4: 4317443$ | $4: 4315716$ | G | A | 4 | ZBTB49 |
| $6: 43325445$ | $6: 43357707$ | G | A | 6 | ZNF318 |
| $16: 49670033$ | $16: 49636122$ | C | A | 16 | ZNF423 |
| $8: 37556023$ | $8: 37698505$ | G | T | 8 | ZNF703 |
| $17: 80789793$ | $17: 82831917$ | G | A | 17 | ZNF750 |

Table S2: The heterogeneity of single cells populations of the primary tumors and lymph nodes of patients BC 03 and BC 07 : proportions of tumor cells vs non-tumor cells.

BC03 BC07

|  | Primary tumor | Lymph node | Primary tumor | Lymph node |
| :--- | :---: | :---: | :---: | :---: |
| Non-tumor | 0.55 | 0.81 | 0.52 | 0.5 |
| Tumor | 0.45 | 0.19 | 0.48 | 0.5 |

## FIGURES



Figure S1. Results of fdr2d from the single cells of primary tumor of patient BC03. The contour map represents the statistics from the permutation in 2D local FDR method, and each filled-circle point presents a mutation of a single cell. The red and blue points indicate the tumor cell and non-tumor cell respectively. The significant cell-level mutations with $\mathrm{fdr} 2 \mathrm{~d}<0.2$ and $\mathrm{fdr} 2 \mathrm{~d}<0.05$ are marked by orange and brown squares, respectively.


Figure S2. Results of fdr2d from the single cells of lymph node of patient BC03. The annotation is referred to Figure S1.


Figure S3: The full list of cell-level mutations of both primary tumor (left) and the lymph node (right) of patient BC 03 . The brown and orange indicate the significant mutations with fdr2d $<0.05, \mathrm{fdr} 2 \mathrm{~d}<$ 0.2 , respectively. The light blue presents the insignificant mutations fdr2d $>=0.2$. The dark blue indicates sites with no supporting reads. The red and blue at the column-side-color band (top) refer the tumor and non-tumor groups of cells, respectively.


Figure S4: The full list of cell-level mutations of both primary tumor (left) and the lymph node (right) of patient BC07. The annotation is referred to Figure S3.


Figure S5. Results of fdr2d from the single cells of primary tumor of patient BC07. The annotation is referred to Figure S1.


Figure S6. Results of fdr2d from the single cells of lymph node of patient BC07. The annotation is referred to Figure S1.


Figure S7. Results of fdr2d from the single cells of control group of MDA-MB-231 cell line. The annotation is referred to Figure S1.


Figure S8. Results of fdr2d from the single cells of treated group of MDA-MB-231 cell line. The annotation is referred to Figure S1.


SNRPC(6:34730386)
PAK1IP1(6:10702647)
CNIH4(1:224553630)
NCEH1(3:172365720)
PSMC3(11:47446725)
PSMC3(11:47444153)
MKI67(10:129902653)
EIF2B4(2:27587647)
STK38(6:36463589)
ASPM(1:197074117)
MAP7D3(X:135308130)
MSH3(5:80109433)
WNK1(12:970240)
SRRM2(16:2814371) SKIV2L2(5:54640988) TRIO(5:14502720) ZBTB1(14:64989274) TP53(17:7577099) MTBP(8:121458742) C10orf88(10:124692048) HAUS3(4:2238074) LUM(12:91502008) TNFRSF21(6:47251976) UQCRC1(3:48646621) TCF25(16:89972658) BRAF(7:140481417) LONP1(19:5699098) GAS8(16:90108924) TRIO(5:14330953)
TCFL5(20:61488922) GTF3C1(16:27473769) LRIG2(1:113655185) SYNE2(14:64593156) TJP1(15:29997732) TLN1(9:35706092)

Figure S9: The full list of cell-level mutations of control group (left) and the treated group (right) of MDA-MB-231 dataset. The annotation is referred to Figure S3. The red and blue at the column-sidecolor band (top) refer the cells and negative controls (no cells).


Figure S10: Results of fdr2d from the single cells of the glioblastoma dataset. The annotation is referred to Figure S1.


PDGFRA(4:55133837) DYNC1LI 2 (16:66770063) CHD6(20:40162197) LPL(8:19805777) EMP2 1 16:10626930) SGK1 6:134491008 ZNFM189(9:104172634) HLA-B $6: 31324143$ PTEN(10.89692826 DCLRE1C(10:14961515)
KIF2C(1:45223589) KIF2C(1:45223589)
MAGI3 $1: 113988097$ )
SPRED $2(2: 65571869)$ SPRE1 $2(2.69992558)$
TANCFYVE $(2.209163447)$ LSAMP ( $3: 115529092$ ) KIF20A(5:137520545) ENPP7P6(8:12338804) UNKNOWN(9:68414365) CDCA5 (11:64847154 SYTL2(11:85418484)
MESDC2(15:81271542)
HP1BP3(1.21102377) WDR78(1:67356866) NBPF10(1:145323614) UNKNOWN (2:47917935) NAGK (2:71298817) UNKNOWN(2:90464691) HS6ST1 $12: 12902575$
RIF1 $2: 152279407$ ) PLEKHA3 $2: 179368871$ )
RNF123 3.49757680$)$ ARL6IP5 $3: 69139140$ ARAMP $3: 115529088$ PDGFRA(4:55130882) CDH10(5:24492953)
RPS10(6:34392484) UNKNOWN(6:58779088) UNKNOWN(6:58779121
HNRNPA2B1(7.26230765) PTPRZ1(7:121513405)
RIMS2 (8:104897549) NUDT13 10:74886054 ARHGAP42(11:100812325) TIRAP (11:126163138) CSAD (12:53573480) UNKNOWN (13:47040047) EMP2(16:10625789)
NPIPA1(16:15039138) NPIPA1 $16: 15039138$ NDE1 $16: 15818967$ )
SULTA $2(16-28603702)$ TR2 (16.66583977) UNKNOWN(18:108385) MIDN(19:1259072)
POU2F2(19:42595283) CKM (19:45822706) UNKNOWN(22:18883818) UNKNOWN $(22: 18883922$
DNAJB7(22.41256845)
Figure S11: The full list of cell-level mutations of the glioblastoma dataset. The annotation is referred to Figure S3.


Figure S12: The survival analysis of top three mutational genes discovered by SCmut and their combination using the mutation calls of Mutect from the TCGA-GBM data. The dash line and solid line indicate the patients with and without mutations, respectively.

## Detection sensitivity of mutation and coverage threshold

The detection sensitivity depends on statistical power, which in turn depends on the read counts and effect sizes (in this case the underlying mutation rates). So assessing sensitivity from the full matrix of results can be misleading, because a great majority of the matrix entries did not have any reads at all. For example, in BC 03 tumour, there were 85 mutation sites from the bulk-cell WES data for which there was any read in at least one of the 33 cells. If we focus on this $85 \times 33$ matrix ( 2805 entries), there were only 412 entries with least one read, and only 238 entries with more than 20 reads. For those 238 entries there were 43 detected mutations ( $\mathrm{fdr} 2 \mathrm{~d}<0.2$ ), so it is not so sparse (see Figure S13a below). This detection rate corresponds to what we should expect from the bulk-cell data (Figure $\mathbf{4 e}$ in the main text).

Sensitivity is of course not always that low. In fact, for the breast cancer cell-line MDA-MB-231 we used in the manuscript, we achieved sensitivity up to $80 \%$, Figure S13b, compared to $\sim 40 \%$ of the BC03 tumour in Figure S13a. The MDA-MB-231 dataset contains a batch of 82 cells from the control group and another batch of 88 cells treated with metformin (treated group). Assuming the drug did not generate new mutations, which seems reasonable from Figure S13b, the results from control and treated group can be used as validation of each other. Such validation was shown in Section 3.4 of the main text.


Figure S13. Detection rate of mutation and coverage threshold in a) BC03 tumour and b) the breast cancer cell-line (MDA-MB-231) datasets. Detailed calculations for panel (b): In the control group ( $\mathrm{n}=82$ cells), there were 26 confirmed-somatic mutation sites from the COSMIC database (PMID: 27899578) for which there was any read in at least one of the 82 cells. Focusing on this $26 \times 82$ matrix ( 2,132 entries), there were only 414 entries with more than 10 reads, and 268 of those were detected mutations (fdr $2 \mathrm{~d}<0.2$ ). Thus, the proportion of detected mutations is $268 / 414=65 \%$; for entries more than 60 reads the proportion is $\sim 80 \%$. Similar results were obtained in the treated group.

