Recombination Rate Variation Modulates Gene Sequence Evolution Mainly via GC-Biased Gene Conversion, Not Hill–Robertson Interference, in an Avian System

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Abstract

The ratio of nonsynonymous to synonymous substitution rates (\(d_{NS}/d_S\)) is often used to measure the strength of natural selection. However, \(d_{NS}/d_S\) may be influenced by linkage among different targets of selection, that is, Hill–Robertson interference (HRI), which reduces the efficacy of selection. Recombination modulates the extent of HRI but may also affect \(d_{NS}/d_S\) by means of GC-biased gene conversion (gBGC), a process leading to a preferential fixation of G:C (“strong,” S) over A:T (“weak,” W) alleles. As HRI and gBGC can have opposing effects on \(d_{NS}/d_S\), it is essential to understand their relative impact to make proper inferences of \(d_{NS}/d_S\). We used a model that separately estimated S-to-S, S-to-W, W-to-S, and W-to-W substitution rates in 8,423 avian genes in the Ficedula flycatcher lineage. We found that the W-to-S substitution rate was positively, and the S-to-W rate negatively, correlated with recombination rate, in accordance with gBGC but not predicted by HRI. The W-to-S rate further showed the strongest impact on both \(d_{NS}\) and \(d_S\). However, since the effects were stronger at 4-fold than at 0-fold degenerated sites, likely because the GC content of these sites is farther away from its equilibrium, \(d_{NS}/d_S\) slightly decreases with increasing recombination rate, which could falsely be interpreted as a consequence of HRI. We corroborated this hypothesis analytically and demonstrate that under particular conditions, \(d_{NS}/d_S\) can decrease with increasing recombination rate. Analyses of the site-frequency spectrum showed that W-to-S mutations were skewed toward high, and S-to-W mutations toward low, frequencies, consistent with a prevalent gBGC-driven fixation bias.

Key words: gBGC, Hill–Robertson interference, \(d_{NS}/d_S\), divergence, diversity, rate of molecular evolution.

Introduction

Estimation of nucleotide substitution rates in protein coding sequences allows investigating the processes that drive gene sequence evolution. In particular, the ratio of nonsynonymous \((d_{NS})\) to synonymous \((d_S)\) substitution rates (commonly referred to as \(d_{NS}/d_S\)) is a widely used measure that provides information on the strength of natural selection acting on the evolution of protein-coding sequences (Yang and Swanson 2002). However, other processes can also affect substitution rates, including recombination (Webster and Hurst 2012). Everything else being equal, two genes subject to similar selection pressure can yield contrasting \(d_{NS}/d_S\) estimates if they are located in different recombination environments. This is partly because the rate of recombination will affect the extent and character of linked selection, of which the local rate of recombination is a strong determinant. More specifically, linkage between targets of selection reduces the efficacy of selection, known as Hill–Robertson interference (HRI) (Hill and Robertson 1966). It slows down the fixation rate of beneficial variants and thereby the rate of adaptive evolution, resulting in reduced \(d_{NS}/d_S\). At the same time, linkage among sites hinders the action of purifying selection and thus increases the fixation rate of slightly deleterious mutations, resulting in increased \(d_{NS}/d_S\). Given that a predominant part of nonsynonymous mutations are deleterious, a negative relationship between recombination rate and \(d_{NS}/d_S\) may be expected (Haddrill et al. 2007; Betancourt et al. 2009; Hurst 2009; Campos et al. 2014).

Another widespread phenomenon by which recombination rate may affect substitution rates is GC-biased gene conversion (gBGC). gBGC is a process that induces a fixation bias for “strong” nucleotides (S; strong in the sense of the number of hydrogen bonds between base pairs, i.e., three between G and C) over “weak” nucleotides (W; two hydrogen bonds between A and T). More precisely, it acts on sites in the neighborhood of recombination-initiating double-strand breaks (DSBs) that are heterozygous for a strong and a weak nucleotide. These heterozygous sites induce mismatches in heteroduplex DNA, which is formed as part of the repair mechanism of DSBs, that will be repaired more frequently in favor of the G:C allele (Marais 2003; Mancera et al. 2008; Lesecque et al. 2013). Importantly, the nonrandom increase in frequency of G:C alleles is not caused by a difference in fitness of strong relative to weak alleles. However, gBGC resembles the action of natural selection as it influences the probability of fixation of mutations and therefore has direct implications for inferences of natural selection. gBGC can cause an increased probability of fixation of mildly deleterious mutations in coding sequences creating potentially significant negative fitness effects (Duret and Galtier 2009; Glemin 2010; Lartillot 2013a; Lachance and Tishkoff 2014) as well as false inference of positive selection (Berglund...
et al. 2009; Galtier et al. 2009; Ratnakumar et al. 2010). Even though signatures of gBGC are pervasive in many taxa (Romiguier et al. 2010; Escobar et al. 2011; Muyle et al. 2011; Pessia et al. 2012; Lartillot 2013b; Weber et al. 2014; Lassalle et al. 2015; Wallberg et al. 2015), the effect of gBGC on $\omega$ has predominantly been investigated in mammals where a greater impact on nonsynonymous substitutions than on synonymous substitutions is suggested to increase $\omega$ (Galtier et al. 2009; Ratnakumar et al. 2010; Kostka et al. 2012). However, since the relative effect of gBGC on the two substitution classes depends on a multitude of factors, it might generally affect $\omega$ in more complex ways (Capra and Pollard 2011; Lartillot 2013a).

The combined effect of HRI and gBGC mediated through recombination rate variation and their relative importance on estimates of $\omega$ is not immediately obvious. One way of dissecting how recombination affects the inference of selection and disentangling the role of HRI and gBGC is to separately analyze substitutions varying in the degree to which they may be influenced by gBGC (Berglund et al. 2009). Specifically, the rate of weak-to-strong (W-to-S) substitutions can be expected to show a positive, and the rate of strong-to-weak (S-to-W) substitutions a negative, correlation with recombination rate (Duret and Arndt 2008). In turn, this means that correlations between $\omega$ and recombination rate may differ between different mutation categories given the interplay between selection and gBGC.

Here, we analyze the relationship between recombination rate and the rate of molecular evolution in an avian system, and how this relationship is affected by HRI and gBGC. Of particular relevance is that the rate of recombination shows significant variation across the avian genome, more so than in many other vertebrate lineages and that the landscape of recombination rate variation has remained relatively stable over evolutionary time scales, such that signatures of different processes have had time to build up (Mugal et al. 2013; Kawakami et al. 2014). Moreover, GC content at putatively neutrally evolving sites has not yet reached its equilibrium state in avian genomes and typically evolving toward a higher GC content (Nabholz et al. 2011; Weber et al. 2014). It has therefore been suggested that gBGC has had a profound effect on avian genome evolution (Webster et al. 2006; Backstrom et al. 2013; Mugal et al. 2013; Weber et al. 2014). These characteristics represent striking differences to other vertebrate lineages, in particular to primates where GC content at putatively neutrally evolving sites is on average declining (Duret et al. 2006; Romiguier et al. 2010). In this study, we benefit from a well-annotated genome sequence of high assembly quality of the collared flycatcher (Ficedula albicollis). This, along with the access to a detailed recombination rate map and polymorphism data from whole-genome resequencing of population samples of this species, gives us unusual power to study how recombination modulates sequence evolution in an avian system. Our results suggest that $\omega$ can be a misleading measure for making inference of selection if gBGC is not properly accounted for and that HRI has a minor influence on gene sequence evolution in this avian system.

### Results

#### The Impact of Recombination Rate, GC Content, and Exon Density on Rates of Molecular Evolution

To investigate patterns of substitution and their interplay with different genomic properties, we aligned 8,423 one-to-one orthologous gene sequences from the genomes of collared flycatcher (F. albicollis), zebra finch (Taeniopygia guttata), and chicken (Gallus gallus). We binned genes according to the rate of recombination into 21 bins and concatenated exons within each of the bins to reduce noise in the estimates of substitution rates. We estimated $d_{Wu}$, $d_{S}$, and $\omega$ in the flycatcher lineage using the phylogeny ([chicken](zebra finch, flycatcher)). To investigate the impact of HRI and gBGC on these estimates, we performed a multiple linear regression analysis with three different candidate explanatory variables: 1) pedigree-based recombination rate, the primary parameter of interest, 2) exon density, as a proxy of the density of targets of selection, which impacts the strength of HRI, and 3) GC content at 4-fold degenerated sites (GC$_4$) as a proxy of long-term recombination rate, since recombination may impact GC content through the process of gBGC (Meunier and Duret 2004; Duret and Galtier 2009). Indeed, there was a strong correlation between recombination rate and GC$_4$ (Pearson correlation coefficient $r = 0.854$, $P = 8.69 \cdot 10^{-7}$).

The multiple linear regression analysis revealed no significant relationships between $d_{Wu}$ and any of the candidate explanatory variables. On the other hand, $d_{S}$ showed a positive relationship with GC$_4$ and a slightly negative relationship with exon density (table 1). We would not expect any of these variables to affect the putatively neutral substitution rate (i.e., $d_{S}$) via the action of HRI. Strong gBGC could explain the observed relationship between $d_{S}$ and GC$_4$, since gBGC increases the fixation probability of GC alleles, which would lead to a simultaneous increase of substitution rate and GC content. Alternatively, selection on codon usage could lead to a relationship between GC content and $d_{S}$. However, there is no clear evidence for selection on codon usage in birds (Rao et al. 2011; Wang et al. 2014). We also found a significant negative relationship between $\omega$ and GC$_4$ (table 1), which could indicate the action of HRI. However, given that $d_{S}$ is affected by GC$_4$, caution might be required to interpret the relationship between GC$_4$ and $\omega$ as the action of HRI. By a more detailed analysis, we demonstrate below that this would actually be a false conclusion.

#### The Impact of gBGC on Rates of Molecular Evolution

To explore the possible role of gBGC in determining rates of molecular evolution, we applied a strand-symmetric model (Lobry 1995) implemented in the BppML package of the Bio++ suite program (Dutheil and Boussau 2008). This model allowed us to estimate specific substitution rates for the four different mutation categories X-to-Y, corresponding to the substitution rates X-to-Y for any of the four possible (W, S) combinations, namely strong-to-strong (S-to-S), S-to-W, W-to-S, and weak-to-weak (W-to-W), where weak bases are A and T and strong bases are G
Interestingly, similar correlations for S-to-S and W-to-W and another parameter that we did not consider.

Figure 1 demonstrates that the rate of W-to-S substitution was far higher than any of the rates for the other three mutation categories. This applies particularly for 4-fold degenerated sites, where the relative contribution of the W-to-S substitution rate to the total rate was on average 46%, whereas S-to-W substitutions contribute only 25%. As a consequence, the W-to-S substitution rate largely governed $d_s$. Indeed, the relationship between $d_s$ and recombination rate was very similar to that between the W-to-S substitution rate and recombination rate (fig. 1B, table 2). The same was true for 0-fold degenerated sites where the relative contributions of W-to-S and S-to-W were 46% and 30%, respectively (fig. 1A). In conclusion, our results show that W-to-S substitutions largely determine both the nonsynonymous and the synonymous substitution rate. The W-to-S substitution rate increases with the rate of recombination, consistent with the hypothesis that strong gBGC raises the total substitution rate.

Estimates of $\omega$ over the four mutation classes combined showed a marginally significant negative correlation with recombination rate and the same was observed for the W-to-S substitution rate ratio (fig. 1C). On the contrary, the S-to-W rate ratio was strongly positively correlated with recombination rate, whereas S-to-S and W-to-W rate ratios showed no correlation with recombination rate (fig. 1C, table 2). Interestingly, we found a difference in $d_N$ and $\omega$ estimates between the nonrecombining bin and the bins with low recombination in all four mutation categories (fig. 1A and C). This difference may reflect the role of HRI in nonrecombining regions. In contrast, if HRI was determining patterns of $\omega$ throughout the whole range of recombination rate variation, we would expect a negative correlation between $d_N$ and recombination rate, which was not observed in our data. On the contrary, we observed a positive correlation between $d_N$ and recombination rate, which argues for a stronger impact of gBGC in determining $d_N$.

If recombination governs the rates of molecular evolution by means of gBGC, this should be reflected in the evolution of the GC content (Galtier et al. 2001; Meunier and Duret 2004; Duret and Arndt 2008). Specifically, the equilibrium GC content (GC$^*$), which represents the GC content that would be reached at equilibrium if estimated substitutions rates where invariant over time, can be used as a proxy for the strength of gBGC. The current GC content on the other hand reflects the accumulated effect of gBGC over the past. Provided that the recombination landscape is evolutionary stable, such that signatures of gBGC can accumulate over time, both current GC content and GC$^*$ are expected to be positively correlated with recombination rate. Indeed, we observe that recombination rate is strongly positively correlated with current GC content (fig. 2A) ($r = 0.84$, $P = 1.95 \times 10^{-06}$ and $r = 0.854$, $P = 8.69 \times 10^{-07}$ for 0-fold and 4-fold degenerated sites, respectively) as well as the GC$^*$ (fig. 2B) ($r = 0.841$, $P = 1.8 \times 10^{-06}$ and $r = 0.892$, $P = 5.62 \times 10^{-08}$ for 0-fold and 4-fold degenerated sites, respectively). Moreover, we found that the difference between GC$^*$ and current GC content ($\Delta$GC) is positive (GC$^*$ > GC) in all recombination bins (fig. 2C). As $\Delta$GC measures the distance

### Table 1. Linear Regression t Values and $P$ Values for $d_N$, $d_S$, and $\omega$ as a Function of Recombination Rate, Exon Density, and GC$_d$.

<table>
<thead>
<tr>
<th>Explanatory variable</th>
<th>$d_N$</th>
<th>$d_S$</th>
<th>$\omega$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Recombination rate</td>
<td>0.61</td>
<td>0.75</td>
<td>0.61</td>
</tr>
<tr>
<td>$GC_d$</td>
<td>1.96</td>
<td>6.78</td>
<td>2.21</td>
</tr>
<tr>
<td>Gene density</td>
<td>-0.49</td>
<td>-0.55</td>
<td>0.81</td>
</tr>
<tr>
<td>Multiple R$^2$</td>
<td>0.63</td>
<td>0.92</td>
<td>0.38</td>
</tr>
</tbody>
</table>
of the current GC content to its equilibrium value, this suggests that GC content is still increasing and that gBGC leads to an overall increase of substitution rates. It is true for both 0-fold and 4-fold degenerated sites, where 4-fold degenerated sites are further away from their equilibrium than 0-fold degenerated sites (ΔGC4 > ΔGC0). The greater distance of the current GC content to its equilibrium at 4-fold degenerated sites when compared with 0-fold degenerated sites could explain why synonymous substitutions are more strongly affected by gBGC than nonsynonymous substitutions.

The Impact of gBGC on Patterns of Diversity

Besides their influence on the rates of molecular evolution, HRI and gBGC can affect patterns of nucleotide diversity. HRI reduces the efficacy of selection in low recombination regions, which is expected to lead to a positive correlation between recombination rate and neutral diversity irrespective of the mutation category (Campos et al. 2014). Moreover, HRI is not expected to affect the site frequency spectrum (SFS) of the four mutation categories in different directions. On the other hand, the impact of gBGC on patterns of diversity should differ between mutation categories. Importantly, gBGC skews the SFS of W-to-S mutations toward high frequencies and of S-to-W mutations toward low frequencies (Capra et al. 2013; Lachance and Tishkoff 2014; Wallberg et al. 2015). To better distinguish between HRI and gBGC, we therefore also analyzed diversity levels and the SFS of the four different mutation categories. We investigated nucleotide diversity in protein-coding genes based on data from whole-genome resequencing of 20 collared flycatchers from an allopatric population. Using the same set of 8,423 genes that were used for substitution rate estimates, we analyzed a total number of 8,460,789 sites (6,934,131 0-fold and 1,526,658 4-fold degenerated sites), of which we identified 33,581 as polymorphic (14,354 0-fold and 19,227 4-fold degenerated sites); this represents an unusually large data set for coding sequence polymorphisms from a natural population. We calculated Watterson’s θ (θW) and the unfolded SFS for each of the S-to-S, S-to-W, W-to-S, and W-to-W mutation categories and distinguished 0-fold from 4-fold degenerated sites. The SFS showed a right skew and higher proportion of high-frequency derived variants for the W-to-S class, and a higher proportion of low-frequency derived alleles for the S-to-W class, which points to a strong impact of gBGC on patterns of diversity. This holds true both at 4-fold (fig. 3A) and 0-fold degenerated sites (supplementary fig. S1A, Supplementary Material online). Illustrations of the relative SFS for each class clearly visualize a strong shift in the relative proportion
Estimates of S-to-W and W-to-S derived mutations (fig. 3B and supplementary fig. S1B, Supplementary Material online). Estimates of θ\textsubscript{W} showed no significant relationship with recombination rate at 0-fold degenerated sites for any mutational class or for total θ\textsubscript{W} (fig. 4A, table 3). For 4-fold degenerated sites, there was a positive and statistically significant correlation only between W-to-S-specific θ\textsubscript{W} and recombination rate (fig. 4B, table 3), compatible with an influence of gBGC on patterns of diversity. The W-to-S-specific ratio of θ\textsubscript{W} at 0-fold and 4-fold degenerate sites showed a negative correlation with recombination, which should at least in part be driven by the positive correlation between W-to-S-specific θ\textsubscript{W} and recombination rate. We found no correlation between W-to-W-specific and S-to-S-specific θ\textsubscript{W} estimates with recombination rate (fig. 4, table 3).

Finally, estimates of θ\textsubscript{W} indicate that S-to-W mutations are the most prevalent mutations across all recombination bins (fig. 4A and B). We estimated the mutational bias (\(R_p\)) for S-
...to W and W-to-S as the ratio of the rate of singletons of each mutation category. The average \( R_{s,4} \) at 4-fold degenerated sites across all recombination bins was 3.41. This suggests that the observed substitution bias for W-to-S is not driven by a mutational bias but a fixation bias.

**Theoretical Insights on the Interaction between gBGC and Natural Selection**

To better understand the consequences of recombination via gBGC on rates of molecular evolution, we analytically described the impact of gBGC on substitution rates at neutrally evolving sites (reflecting synonymous substitution rates) as well as sites evolving under natural selection (reflecting nonsynonymous substitution rates). The strength of gBGC was modeled by the coefficient of gBGC (\( b \)), which correlates linearly with the recombination rate and affects the probability of fixation similar to the coefficient of selection (\( s \)) (for details, see Materials and Methods). Thus, similar to the action of selection, the degree by which \( b \) affects the rate of molecular evolution depends directly on \( N_e \). The larger \( N_e \) the stronger is the effect of gBGC, which can be expressed as the population scaled coefficient of gBGC, \( B = 4N_e b \).

We allowed \( B \) to vary from 0 to 8 to cover strengths of gBGC corresponding to a wide range of \( GC^* \), encompassing the range found in the flycatcher lineage (fig. 5D). The mutation rate was approximated by the rate of singletons at 4-fold degenerated sites and therefore differed between mutation categories (fig 4B). To model molecular evolution at sites evolving under natural selection, an estimate of the distribution of fitness effects (DFE) is required, knowledge of which is limited in birds. We therefore made the simplifying assumption that the DFE is represented by three categories: 1) lethal mutations, that is, mutations that are immediately removed by selection and do not appear as polymorphic sites; 2) slightly deleterious mutations, and 3) slightly advantageous mutations. We approximated the proportion of lethal mutations as \( 1 - \) [the ratio of the total singleton rate at 0-fold degenerated sites to the total singleton rate at 4-fold degenerated sites], which was 0.78. For the remaining two categories, 90% of the mutations were assigned to be slightly deleterious, while only 10% were assigned to be slightly advantageous.

The strength of the population scaled selection coefficient was assumed to be the same for deleterious and advantageous mutations (\( |N_e s| \leq 1 \)). These parameters led to lower \( GC^* \) at selected than at neutrally evolving sites, consistent with the pattern found in the flycatcher lineage. To explore the impact of current GC content (or, more specifically, of \( \Delta GC \)) on patterns of molecular evolution we applied four different scenarios: 1) the current GC is at equilibrium (\( GC = GC^* \), i.e., \( \Delta GC = 0 \)) and synonymous and nonsynonymous sites have their own equilibria (as shown in fig. 5D), 2) current GC = 0.2 and \( \Delta GC > 0 \) regardless of the value of \( B \), 3) current GC = 0.5 and \( \Delta GC \) is either positive or negative,
and 4) current $GC = 0.9$ and $\Delta GC < 0$ except for extremely high values of $B$ where $GC^*$ is close to 1. Specifically, this allowed us to assess how $d_N$, $d_S$, and $\omega$ can vary with the strength of $gBGC$ depending on how far the GC content is from the equilibrium value.

The model shows that both $d_N$ and $d_S$ will increase with increasing $B$ whenever the current GC content is lower than $GC^*$ ($\Delta GC > 0$), as found in the flycatcher lineage. On the contrary, if the current GC content is higher than the $GC^*$, $d_N$ and $d_S$ may decrease (fig. 5A and B). Figure 5 shows that depending on the current GC content and how far it is from $GC^*$, the difference in the impact of $gBGC$ on $d_N$ and $d_S$ can create both positive and negative relationships between $B$ and $\omega$ (fig. 5D), and thus between recombination rate and $\omega$. On the basis of this model, we argue that $gBGC$ may lead to reduced $\omega$ in high recombining regions under the conditions that $\Delta GC$ is positive and higher at neutrally evolving sites than in sites evolving under natural selection, as found in the flycatcher lineage (fig. 2C). Therefore, the impact of $gBGC$ on the total nonsynonymous and synonymous substitution rates is not only governed by the GC content but even more so by the difference between the current GC content and $GC^*$. The effect of $gBGC$ on substitution rates of each mutational class is visualized in supplementary figure S2, Supplementary Material online.

**Discussion**

We explored the impact of recombination rate variation via HRI and $gBGC$ on inferences of natural selection in an avian model system. Specifically, we addressed the question if HRI and/or $gBGC$ govern the relationship between recombination rate and $\omega$. Since in mammals $gBGC$ has previously been
found to increase $\omega$ (Berglund et al. 2009; Galtier et al. 2009; Ratnakumar et al. 2010), the weak negative relationship found in the flycatcher lineage seems to point toward a prominent role of HRI in this lineage. However, estimation of lineage-
specific substitution rates for 0-fold and 4-fold degenerated sites for four different mutation categories that are differently affected by gBGC provided evidence for a strong impact of gBGC on rates of molecular evolution. In contrast, the role of HRI in determining genome wide patterns of molecular evolu-
tion seemed comparatively weak. Analyses of patterns of
diversity, including the SFS, of different mutation categories revealed similar conclusions.

In an effort to explain the discrepancies between our find-

ings and earlier studies, we identified $\Delta g$ as an important
determinant of the impact of gBGC on both $d_{\text{N}}$ and $d_{\text{S}}$. It follows that the relative strength of gBGC on nonsynonymous
and synonymous substitutions, as given by differences in
$\Delta g$ between 0-fold and 4-fold degenerated sites, deter-
mines the impact of gBGC on $\omega$. In the flycatcher genome,
the GC content is below the equilibrium value, and both
$\Delta g_{\text{C}}$ and $\Delta g_{\text{G}}$ are positive. $\Delta g_{\text{C}}$ is on average larger
than $\Delta g_{\text{G}}$, suggesting a stronger impact of gBGC on synon-
ymous than on nonsynonymous substitutions. In line with
this notion, our analytical description of the gBGC process
shows that if neutrally evolving sites are further away from
their equilibrium than sites evolving under natural selection,
$\omega$ can decrease with increasing recombination rate. This
seems at first glance surprising since previous studies have
reported that gBGC will in most scenarios have a greater
impact on nonsynonymous substitutions than on synony-
ymous substitutions, leading to an increase of $\omega$ with increas-
ing recombination rate (Galtier and Duret 2007; Duret and
Galtier 2009; Galtier et al. 2009; Ratnakumar et al. 2010). For
example, Galtier et al. (2009) also analytically described gBGC
and showed that in primate lineages gBGC increases $\omega$ under
most conditions. However, this study did not explore the
possibility of $\Delta g_{\text{C}}$ being larger than $\Delta g_{\text{G}}$ and did not
allow for both to be positive, as here observed in the avian
data.

Our analysis of the rate of molecular evolution in the fly-
catcher lineage demonstrates that gBGC may influence infer-
ces of selection in unexpected ways. Specifically, a higher
impact of gBGC on synonymous than on nonsynonymous
substitutions may not lead to the expected increase in $\omega$ as
found in primates where GC$_{4}$ is on average declining but on
the contrary lead to a decrease in $\omega$. This problem should be
common to organisms in which base composition evolves
toward higher GC content. We therefore strongly advise
against interpreting observed relationships between gene se-
quence evolution and recombination without properly ac-
counting for gBGC. For example, a recent study on the
rates of molecular evolution in two passerine bird lineages
(great tit, Parus major, and zebra finch) proposed that the
observed negative relationship between $\omega$ and recombina-
tion rate was owing to a large effect of HRI (Gossmann et al. 2014).
However, this study only vaguely investigated the impact of
gBGC on patterns of $\omega$. Although we observed a weak neg-
ative correlation between recombination rate and $\omega$, our
results widely support the hypothesis that the reduction in
$\omega$ in high recombination regions is mainly the result of a
strong impact of gBGC, which affects nonsynonymous and
synonymous substitutions to a different extent.

In conclusion, our work stresses the importance of inves-
tigating different groups of organisms to gain a better under-
standing of the general mechanism by which gBGC influences
rates of molecular evolution. As shown here, differences in
the recombination landscape, $N_e$ and $\Delta g$ among species may
lead to different signatures of gBGC on $d_{\text{N}}, d_{\text{S}}$ and $\omega$. In birds,
the generally high but at the same time heterogeneous rate of
recombination, along with a stable recombination landscape
and large $N_e$, may have allowed gBGC to show a particularly
strong impact on substitution rates.

**Materials and Methods**

**Sequence Data**

We retrieved putative 1:1 orthologous genes of collared fly-
catcher, zebra finch, and chicken through the Biomart re-
trieval tool in Ensembl release 73 (Kasprzyk 2011; Flicek
et al. 2014). Codon-based alignments were generated using
PRANK (v.130410) (Loytynoja and Goldman 2005). The
Heads-or-Tails (HoT) algorithm implemented in the program
Guidance was used to calculate alignment confidence scores
that reflect alignment uncertainties (Landan and Graur 2007;
Penn et al. 2010). Using default settings, misaligned columns
were discarded. We excluded genes if the length of the coding
sequence was shorter than 200 bp, if the genomic location
was unknown, sex linked, or in microchromosomes with less
than 5 Mb of assembled sequence (chromosomes LG22, 25
and Fal3S; due to limited amount of data) according to the
FicAlb1.5 assembly version of the collared flycatcher genome
(Kawakami et al. 2014). We also excluded genes that had
overlapping transcripts as a result of antisense transcription
and genes with premature STOP codons.

**Estimation of Genomic Features**

We obtained recombination rate estimates in cM/Mb for nonoverlapping 200 kb windows of the collared flycatcher
genome from Kawakami et al. (2014). Recombination rate
values for each ortholog were assigned by mapping genes
to these windows. When a gene covered two or more win-
dows, we calculated a weighted average of the recombina-
tion rates in the corresponding windows. The same approach
was used for assigning exon density values (the proportion of
coding base pairs in the assembled sequence in each
window). Genes were grouped and concatenated into 21 bins based on their recombination rate. Every bin contained
approximately the same number of genes (403 or 404) except
for bin 0 that contained all autosomal genes with recombi-
nation rate estimates of 0 cM/Mb (348 genes). Mean values of
recombination rate in the 20 nonzero categories ranged from
0.176 cM/Mb to 15.535 cM/Mb.

**Estimation of Rates of Molecular Evolution**

We used the codeml program in the phylogenetic analysis by
maximum likelihood (PAML4.7) package (Yang 1997) to
estimate rates of nonsynonymous ($d_{ln}$) and synonymous ($d_{s}$) substitutions for each recombination bin. We used a free-ratio-model (model = 1) to estimate the flycatcher lineage-specific $d_{ln}$, $d_{s}$ and their ratio ($\omega$), assuming a constant $\omega$ over all sites and different equilibrium nucleotide frequencies for each codon position (F3x4) (Yang and Swanson 2002). To assess the potential role of gBGC in the evolution of base composition and substitution rates, we used a strand-symmetric model (Lobry 1995) implemented in the package BppML in the Bio++ suite program (Dutheil and Boussau 2008). This model is nonreversible and thereby allows for the estimation of substitution rates of S-to-S, S-to-W, W-to-S, and W-to-W mutation categories. Flycatcher branch-specific estimates for concatenated genes per recombination bin were made separately for 0-fold and 4-fold degenerated sites. The model also allowed us to estimate the branch-specific GC*, including GC0* and GC4* (GC* of 0-fold and 4-fold degenerated sites, respectively). Analyses using 2nd and 3rd codon positions instead of 0-fold and 4-fold degenerated sites provided similar results (not shown).

Estimation of Diversity and SFS Analysis

We retrieved single-nucleotide polymorphism data from 20 individuals of an Italian population of collared flycatchers (Burri et al. 2015) to investigate potential signatures of gBGC on the SFS. Briefly, whole-genome resequencing of unrelated birds was done using Illumina technology. Reads were mapped to the collared flycatcher genome assembly version FicAlb1.5 (Kawakami et al. 2014) using Burrows-Wheeler Aligner 0.7.4 (Li and Durbin 2009), and variant calling was performed using the Genome Analysis Toolkit (GATK) 2.8-1 (McKenna et al. 2010). We filtered polymorphic sites according to a minimum mapping quality of 20 and minimum variant quality of 15. Additionally, we required at least 12 genotypes with minimum coverage of 5x per individual. We then randomly choose 24 alleles from the genotypes passing the filtering criteria to constantly obtain the same sample size for each site.

We assigned polymorphic sites into one of the different mutation categories described above (S-to-S, S-to-W, W-to-S, and W-to-W). We polarized variant sites using the genome sequence of two outgroup species, Ficedula parva and Ficedula hyperythra (Burri et al. 2015). We defined the ancestral state when the same allele was fixed in at least two of the three species. To ensure low error rates in polarization, we removed sites where more than one species was polymorphic or had missing data. Nonbiallelic positions and codons with more than one polymorphic site were discarded. We estimated $\theta_w$ per site separately for 0-fold and 4-fold degenerated sites for each of the four mutation categories as the ratio of the number of polymorphic sites of each class to the product of the harmonic mean of the sample size and the number of total potential sites for that class (i.e., S-to-W-specific $\theta_w$ was defined as the number of S-to-W polymorphic sites divided by the product of the harmonic mean and the total number of “strong” or G/C sites passing the filtering criteria). We calculated the unfolded SFS separately for 0-fold and 4-fold degenerated sites to compare the distributions of derived allele counts of the different polymorphism classes.

To test for potential differences in mutation rate across different recombination environments, we calculated the rate of singletons for different mutation categories as the ratio of the number of singletons of each class to the total number of potential sites for that class. We also examined the mutational bias ($R_{w}$) between different mutational categories by considering the ratio of S-to-W to W-to-S singleton rates at 4-fold degenerated sites.

Statistical Analyses

We used R version 3.0.1 (R Core Team 2013) to perform all statistical testing. Multiple linear regression analyses were performed with recombination rate, exon density, and GC4 as explanatory variables, and $d_{ln}$, $d_{s}$, and $\omega$ as response variables. Explanatory variables were transformed to minimize the skew in their distribution. Specifically, recombination rate values were log10 transformed after adding 1 to all values, while GC4 and exon density were transformed by using square root transformation. These values were then Z-transformed, which means scaling the data to standardize the mean value to 0 and standard deviation to 1. We computed Pearson correlation coefficients to assess correlation between variables.

The 95% confidence intervals (CIs) were obtained by generating 100 bootstrap replicates of aligned sequences for each recombination bin. For each of these replicates, we estimated the parameters of interest. The standard error (SE) for each parameter was estimated as the standard deviation of the resampling distribution. We then estimated the CIs as the 2.5th and 97.5th percentiles of the Student t distribution. For substitution rates estimated with codeml, we relied on the SE provided by the software and estimated CIs as specified above.

A Mathematical Model of gBGC

Let $u_{X \rightarrow Y}$ represent the substitution rate from X-to-Y, where the pair (X, Y) represents any of the four combinations of W and S. Then substitution rate $u_{X \rightarrow Y}$ can be expressed as a function of the effective population size $N_e$, the particular mutation rate $\mu_{X \rightarrow Y}$ and the probability of fixation $p_{X \rightarrow Y}$.

$$u_{X \rightarrow Y} = 2N_e \cdot \mu_{X \rightarrow Y} \cdot P_{X \rightarrow Y}. \quad (1)$$

Consider a mutation at a selectively neutral site, where the probability of fixation of the segregating polymorphism is not influenced by natural selection. Then gBGC influences the dynamics of the segregating polymorphism just like directional selection (Nagylaki 1983). However, gBGC only impacts the probability of fixation of W-to-S and S-to-W mutations but not the other types of mutations. So the probability of fixation of W-to-W and W-to-S mutations is $1/2N_e$ while the probability of fixation of W-to-S mutations is

$$p_{W \rightarrow S} = \frac{1 - e^{-2b}}{1 - e^{-4N_e b}} \quad (2)$$
and that of S-to-W mutations is

\[ P_{S\to W} = \frac{1 - e^{2b}}{1 - e^{4N_b}}, \] (3)

where \( b \) represents the coefficient of gBGC. On the other hand, for a mutation under selection, the dynamics of the segregating polymorphism might be influenced by an interplay of selection and gBGC. The probability of fixation of W-to-W and S-to-S mutations remains unaffected by gBGC,

\[ P_{W\to W} = P_{S\to S} = \int \frac{1 - e^{-2s}}{1 - e^{-4N_b}} \phi(s) ds, \] (4)

where \( s \) represents the selection coefficient and \( \phi(s) \) represents the DFE. The probability of fixation of W-to-S mutations is affected by gBGC,

\[ P_{W\to S} = \frac{1 - e^{2(b+s)}}{1 - e^{4N_b(b+s)}} \phi(s) ds \] (5)

as well as that of S-to-W mutations,

\[ P_{S\to W} = \frac{1 - e^{2(b+s)}}{1 - e^{4N_b(b+s)}} \phi(s) ds. \] (6)

Now, let \( u \) represent the overall substitution rate per site. Then \( u \) can be expressed as the sum of the different categories of nucleotide substitution rates weighted by their respective opportunities of mutation, that is, the GC content (\( x_{GC} \)),

\[ u = (1 - x_{GC}) \cdot (u_{W\to S} + u_{W\to W}) + x_{GC} \cdot (u_{S\to W} + u_{S\to S}). \] (7)

Combining equations (1)–(3) and (7) for the neutral scenario leads to

\[ u = 2N_e \cdot \left[ (1 - x_{GC}) \cdot \mu_{W\to S} \cdot \frac{1 - e^{-2b}}{1 - e^{-4N_b(b+s)}} + x_{GC} \cdot \mu_{S\to W} \cdot \frac{1 - e^{2b}}{1 - e^{4N_b}} \right] + [(1 - x_{GC}) \cdot \mu_{W\to W} + x_{GC} \cdot \mu_{S\to S}]. \] (8)

For a scenario that invokes natural selection we combine equations (1) and (4)–(7), which leads to

\[ u = 2N_e \cdot \left[ \int \left( (1 - x_{GC}) \cdot \mu_{W\to S} \cdot \frac{1 - e^{-2(b+s)}}{1 - e^{-4N_b(b+s)}} + x_{GC} \cdot \mu_{S\to W} \cdot \frac{1 - e^{2(b+s)}}{1 - e^{4N_b(b+s)}} + \frac{1 - e^{-2s}}{1 - e^{-4N_b}} \right) \phi(s) ds \right] \] (9)

Further, GC* can be expressed as a function of the substitution rates from W-to-S and S-to-W

\[ GC^* = \frac{u_{W\to S}}{u_{W\to S} + u_{S\to W}}. \] (10)

Combining equations (1)–(3) and (10) for the neutral scenario leads to

\[ GC^* = \frac{1}{1 + R_{\mu} \cdot e^{2(b+1-2N_e)}}. \] (11)

Combining equations (1), (4)–(6), and (10) for a scenario that invokes natural selection leads to

\[ GC^* = \frac{\mu_{W\to S} \cdot \int \left( \frac{1 - e^{-2(b+s)}}{1 - e^{-4N_b(b+s)}} \phi(s) ds \right)}{\mu_{W\to S} \cdot \int \left( \frac{1 - e^{2(b+s)}}{1 - e^{-4N_b(b+s)}} \phi(s) ds \right) + \mu_{S\to W} \cdot \int \left( \frac{1 - e^{2(b-s)}}{1 - e^{-4N_b(b-s)}} \phi(s) ds \right) \}. \] (12)

**Supplementary Material**

Supplementary figures S1 and S2 are available at Molecular Biology and Evolution online (http://www.mbe.oxfordjournals.org/).

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**References**


