Insights into the kinetics of siRNA-mediated gene silencing from live-cell and live-animal bioluminescent imaging

Derek W. Bartlett and Mark E. Davis*

Chemical Engineering, California Institute of Technology, Pasadena, CA 91125, USA

Received December 2, 2005; Revised and Accepted December 23, 2005

ABSTRACT

Small interfering RNA (siRNA) molecules are potent effectors of post-transcriptional gene silencing. Using noninvasive bioluminescent imaging and a mathematical model of siRNA delivery and function, the effects of target-specific and treatment-specific parameters on siRNA-mediated gene silencing are monitored in cells stably expressing the firefly luciferase protein. In vitro, luciferase protein levels recover to pre-treatment values within <1 week in rapidly dividing cell lines, but take longer than 3 weeks to return to steady-state levels in nondividing fibroblasts. Similar results are observed in vivo, with knockdown lasting ~10 days in subcutaneous tumors in A/J mice and 3–4 weeks in the nondividing hepatocytes of BALB/c mice. These data indicate that dilution due to cell division, and not intracellular siRNA half-life, governs the duration of gene silencing under these conditions. To demonstrate the practical use of the model in treatment design, model calculations are used to predict the dosing schedule required to maintain persistent silencing of target proteins with different half-lives in rapidly dividing or nondividing cells. The approach of bioluminescent imaging combined with mathematical modeling provides useful insights into siRNA function and may help expedite the translation of siRNA into clinically relevant therapeutics for disease treatment and management.

INTRODUCTION

RNA interference (RNAi) refers to the ability of double-stranded RNA (dsRNA) to cause sequence-specific degradation of complementary mRNA molecules. Since its discovery in Caenorhabditis elegans in 1998 (1), it has rapidly attracted attention from researchers in fields ranging from genetics to clinical medicine. A natural intracellular process likely involved in cell-based defense against mobile genetic elements such as viruses and transposons (2), RNAi promises to be an invaluable tool for gene function analysis as well as a powerful therapeutic agent that can be used to silence pathogenic gene products associated with diseases including cancer, viral infections and autoimmune disorders (3–8).

A central component of RNAi is a double-stranded siRNA molecule that is 21–23 nt in length with 2 nt long 3' overhangs (9). These siRNA effector molecules can be introduced into cells directly as synthetic siRNAs or indirectly as precursor long dsRNAs or short-hairpin RNAs (shRNAs). RNA polymerase II- or III-driven expression cassettes can be used for constitutive expression of shRNA molecules (10). Both the long dsRNAs and shRNAs are cleaved by Dicer (RNase III family of endonucleases) into the appropriately sized siRNA effectors. Although the presence of dsRNA >30 nt can elicit an interferon response in mammalian cells (11), Elbashir and co-workers demonstrated that synthetic 21mer siRNAs evaded the interferon response and yet were still effective mediators of sequence-specific gene silencing in mammalian cells (9). Here, we have chosen to focus on the use of synthetic 21mer siRNA duplex molecules in mammalian cells for transient gene silencing.

Because synthetic siRNA molecules must be transported into the cells before they can function in RNAi, successful delivery of siRNA is of central importance. Delivery vehicles must protect the siRNA from nucleases in the serum or extracellular media, enhance siRNA transport across the cell membrane and guide the siRNA to its proper location through interactions with the intracellular trafficking machinery. While naked siRNA molecules have been shown to enter cells, significantly more siRNA can be delivered using carrier vehicles (12,13). Both viral and nonviral vectors deliver siRNA into cells, although viral vectors are limited to...
delivering siRNA-expressing constructs such as shRNA. Commercially available cationic lipids such as Oligofectamine can effectively deliver siRNA molecules into cells in vitro with transfection efficiencies approaching 90% (9). However, the high toxicity of cationic lipids limits their use for systemic delivery in vivo. Recent studies from our laboratory have shown that cyclodextrin-containing polycations (CDPs) can achieve safe and effective systemic delivery of siRNA in mice (14). Here, we consider the nonviral delivery of siRNA using cationic lipids or polymers.

A challenge for the successful application of siRNA will be to determine the dosing schedule required for efficacy, making insights into the kinetics of siRNA-mediated gene silencing foundational for the future clinical use of siRNA. Without a proper understanding of the kinetics of the process and the parameters that can affect the resulting gene silencing, application of RNAi will be governed largely by trial and error. The ability to specifically tailor and optimize the treatment for each particular system would save significant time and resources, especially given the high cost of synthetic siRNA molecules and the amount of material required for in vivo studies. Mathematical modeling using simple kinetic equations for each step in the RNAi process can shed light on many of these questions regarding the kinetic aspects of RNAi. To our knowledge, there are only a few published examples of such studies looking at the kinetics of the intracellular RNAi process (15–18). Of these studies, none has combined the delivery process and the interaction with the RNAi machinery in mammalian cells. Bergstrom and co-workers (15) proposed a unidirectional amplification method in their mathematical model of RNAi-mediated gene silencing. Because no RNA-dependent RNA polymerase has yet been found in mammalian cells, they acknowledged that their model did not address the silencing mechanisms observed in mammals. Groenenboom and co-workers (16) recently proposed a mathematical model for RNAi that contained several extensions to the core RNAi pathway, providing for siRNA degradation by RNase as well as primed amplification. Their model aimed to explain transgene- or virus-induced gene silencing and avoidance of self-reactivity, but did not consider any steps in the delivery process. Similarly, Raab and Stephanopoulos (17) looked at the dynamics of gene silencing by siRNA given at different doses and at various times relative to plasmid transfection, but did not incorporate siRNA delivery. Arciero and co-workers (18) created a mathematical model to investigate tumor-immune evasion and siRNA treatment. Although this model provided insights into how siRNA can be used in cancer treatment, it did not examine the delivery process and there were no experimental data from in vitro or in vivo studies. Here, we use bioluminescent imaging and mathematical modeling to investigate the steps of RNAi from siRNA delivery to intracellular function with the aim of enabling the practical application and design of siRNA-based treatment strategies both in vitro and in vivo. Because the imaging is noninvasive and nondestructive, the same set of cells or animals can be followed for the entire study. These results will complement investigations using more traditional analytical methods to monitor mRNA or protein knockdown and hopefully serve to encourage the rational design of experimental and clinical siRNA-based treatments.

MATERIALS AND METHODS

Production of luciferase-expressing cell lines by lentiviral transduction

Cell lines were incubated with viral supernatant containing SMPU-R-MNCU3-LUC, a lentiviral vector based on HIV-1 that transduces the firefly luciferase gene. The backbone vector SMPU-R has deletions of the enhancers and promoters of the HIV-1 long terminal repeat (SIN), has minimal HIV-1 gag sequences, contains the cPPT/CTS sequence from HIV-1, and has three copies of the UES polyadenylation enhancement element from SV40 and has a minimal HIV-1 RRE [gift from Paula Cannon, Children’s Hospital Los Angeles, Los Angeles, CA (19)]. The vector has the U3 region from the MND retroviral vector as an internal promoter driving expression of the firefly luciferase gene from SP-LUC+ [Promega, Madison, WI (20)].

siRNA duplexes

All siRNA molecules were ordered purified and pre-annealed (‘Option C’) from Dharmacon Research, Inc. (Lafayette, CO). siGL3 (sense, 5’-CUUACGCAGAUCUUCGAdTdT-3’; antisense, 5’-UCGAAGUACUCAGCGUAAdTdT-3’) is an unmodified siRNA duplex that targets the luciferase gene, while siCONTROL non-targeting siRNA #1 (siCON1; sense, 5’-UAGCGACUAACACAUCAAUU-3’; antisense, 5’-UUG-AUGUGUUUAGUCGCUAUU-3’) is an unmodified siRNA duplex bioinformatically designed to minimize the potential for targeting any known human or mouse genes.

In vitro transfections

Cells were seeded in 24-well plates 2–3 days prior to transfection at 2 × 10⁴–1 × 10⁵ cells per well and grown in media supplemented with 10% fetal bovine serum (FBS) and antibiotics (penicillin/streptomycin). The cells were transfected with siRNA using cationic lipids or polymers.

Formation of subcutaneous tumors in mice

Luciferase-expressing Neuro2A (Neuro2A-Luc) cells were grown to confluence in media supplemented with 10% FBS and antibiotics (penicillin/streptomycin). Immediately prior to injection, cells were washed with phosphate-buffered saline (PBS), trypsinized and resuspended in serum-free media at 2 × 10⁶ cells/ml. Each mouse received 0.5 ml of the resulting cell suspension by subcutaneous injection.

Low-pressure tail-vein (LPTV) injection of formulated siRNA polyplexes

All complexes were made with siRNA and an imidazole-modified CDP (CDP-Im) synthesized as described previously (21,22). Before addition to siRNA, CDP-Im was mixed with an adamantane-PEG₅₀₀₀ (AD-PEG) conjugate and an AD-PEG-transferrin (Tf) conjugate such that the total moles of AD-PEG or AD-PEG-Tf equaled the number of moles of β-CD. Tf-targeted polyplexes contained 1% AD-PEG-Tf relative to AD-PEG. This mixture was added to an equal volume
of siRNA at a charge ratio (positive charges from CDP-Im to negative charges from siRNA backbone) of 3:1 (+/−). An equal volume of 10% (w/v) glucose in water was added to the resulting polyplexes to yield a 5% (w/v) glucose (D5W) solution suitable for injection. Each mouse was injected with 200 μl of this polyplex solution containing 50 μg siRNA per 20 g mouse (2.5 mg/kg siRNA).

High-pressure tail-vein (HPTV) co-injection of plasmid and siRNA
Hydrodynamic, or HPTV, injection of nucleic acids can achieve significant levels of nucleic acid in the hepatocytes of mice (23,24). A. McCaffrey and M. Kay kindly donated a plasmid (pApoEHCRLuc) containing the firefly luciferase gene under the control of the human α1-antitrypsin promoter and the apolipoprotein E locus control region. For HPTV co-injection studies in BALB/c mice, each 20 g mouse received a 10% w/v injection of a D5W solution containing 0.25 mg/kg of the luciferase-containing plasmid and 2.5 mg/kg siRNA.

Bioluminescent imaging
Cell culture plates or mice containing the luciferase-expressing cells were imaged using the Xenogen IVIS 100 Imaging System (Xenogen, Alameda, CA). D-luciferin (Xenogen) was dissolved in PBS at 15 g/l. For in vitro assays in 24-well plates, 50 μl of the 15 g/l luciferin solution was added to each well containing 1 ml of media. Light emission was measured 2–3 min after addition of the luciferin. For in vivo experiments, 0.2 ml of the 15 g/l luciferin solution was injected intraperitoneally 10 min before measuring the light emission. Mice were anesthetized with an initial dose of 5% isoflurane followed by a maintenance dose of 2.5% isoflurane. Bioluminescent signal intensities were quantified using Living Image software (Xenogen).

Mathematical model
The model presented here was designed to allow the user to specifically study the impact of parameter values on gene silencing by RNAi. When designing an siRNA-based treatment, the main controllable parameters are the delivery method (naked siRNA, formulated with vector, chemically modified) and dosing schedule. These choices must be governed by parameters such as the target mRNA half-life, target protein half-life, threshold for reduction (in either target mRNA or protein), number of target cells and desired knockdown duration. The model’s design criteria therefore included the ability to enable user-defined values for these parameters that characterize each experimental system.

A simplified schematic of the major processes included in the model is shown in Figure 1. Model variables (Table 1) and parameters (Table 2) were used to develop a set of ordinary differential equations for the steps involved in siRNA delivery to and function within mammalian cells in vitro and in vivo. The differential equations governing each major process from the delivery of siRNA to its intracellular interaction with the RNAi machinery are grouped into modules that can be changed independently to modify the model complexity as desired. A detailed description of the mathematical model and the rationale for its design are provided in the Supplementary Data.
Table 1. Model variables

<table>
<thead>
<tr>
<th>Name</th>
<th>Model compartment</th>
<th>Description (units)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bcf</td>
<td>Plasma</td>
<td>Free complex in circulation (# vol⁻¹)</td>
</tr>
<tr>
<td>Bcb</td>
<td>Plasma</td>
<td>Bound complex in circulation (# vol⁻¹)</td>
</tr>
<tr>
<td>Ec</td>
<td>Extracellular</td>
<td>Extracellular complex in local vicinity (# vol⁻¹)</td>
</tr>
<tr>
<td>Enc</td>
<td>Intracellular</td>
<td>Endosomal complex (# vol⁻¹)</td>
</tr>
<tr>
<td>Enna</td>
<td>Intracellular</td>
<td>Endosomal free siRNA (# vol⁻¹)</td>
</tr>
<tr>
<td>Cc</td>
<td>Intracellular</td>
<td>Cytoplasmic complex (# vol⁻¹)</td>
</tr>
<tr>
<td>Cna</td>
<td>Intracellular</td>
<td>Cytoplasmic free siRNA (# vol⁻¹)</td>
</tr>
<tr>
<td>R</td>
<td>Intracellular</td>
<td>Activated RISC complex bound to mRNA (# vol⁻¹)</td>
</tr>
<tr>
<td>C</td>
<td>Intracellular</td>
<td>Activated RISC complex bound to mRNA (# vol⁻¹)</td>
</tr>
<tr>
<td>M</td>
<td>Intracellular</td>
<td>Target mRNA (# vol⁻¹)</td>
</tr>
<tr>
<td>P</td>
<td>Intracellular</td>
<td>Target protein (# vol⁻¹)</td>
</tr>
<tr>
<td>Z</td>
<td>Intracellular</td>
<td>Number of cells (#)</td>
</tr>
</tbody>
</table>

Cell growth and target protein production

\[
\frac{dZ}{dt} = kgrowth \cdot Z \left(1 - \frac{Z}{Z_{\text{max}}}\right)
\]

All of the equations for intracellular siRNA-associated species contain a term to account for dilution due to cell division, where dilution is equal to the ratio of new cells divided by the total number of cells. For example, if the number of cells doubles in 1 day, then dilution would equal 0.5 and the concentration of the intracellular species would likewise be reduced by 50%. For the sake of calculation simplicity, only species involving the delivered siRNA molecules are diluted by this factor; all other intracellular species (i.e. target mRNA and target protein) are assumed to not change after cell division because they are produced intracellularly by both of the daughter cells. The net effect of this is that the siRNA-associated species are diluted equally between the two daughter cells after each cell division.

The set of ODEs was solved with MATLAB (The MathWorks, Inc., Natick, MA) using the stiff ODE15s solver. The ODE15s solver is a variable-order solver based on the numerical differentiation formulas. Parametric sensitivity analysis was performed using SENS_SYS written by V. M. Garcia Molla. This MATLAB routine is an extension to the ODE15s solver that calculates the derivatives of the solution with respect to the parameters.

RESULTS

In vitro and in vivo experiments were conducted to gain insights into the general kinetics of siRNA-mediated gene silencing in cell lines that constitutively express the luciferase gene. Constitutively expressed genes, in contrast to genes expressed transiently by plasmids, provide a more realistic model for clinical application in which an endogenous gene, such as an oncogene, is the target for a therapeutic siRNA. The Xenogen IVIS 100 Imaging System allowed us to monitor luciferase activity in luciferase-expressing cells growing in 24-well plates or present in subcutaneous tumors or livers in live mice; because the imaging was noninvasive, luciferase activity was measured in the same plate of cells or the same animals over the entire duration of the study. Monitoring the kinetics of siRNA-mediated gene silencing in the same population of cells helps to avoid variability introduced when using different cell populations for each time point as required in luminometer-based luciferase detection or flow cytometry (for fluorescent reporters). Additionally, firefly luciferase has a short half-life of ~2 h, so that its level should change concomitantly with the level of mRNA (25,26). This enables the use of bioluminescent imaging of luciferase protein activity as an indicator of mRNA transcript degradation by the delivered siRNA molecules.

Effect of siRNA dose on luciferase knockdown in vitro

The amount of siRNA applied to the extracellular media has a significant impact on the magnitude of the gene silencing but a
Table 2. Model parameters

<table>
<thead>
<tr>
<th>Name</th>
<th>Description (units)</th>
<th>Determination</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>max</td>
<td>Maximum number of cells (#)</td>
<td>Determined experimentally</td>
<td>Fit to each system</td>
</tr>
<tr>
<td>partition</td>
<td>Effective fraction of dose available to target cells</td>
<td>Estimated from experimental data</td>
<td>$1 \times 10^{-5}$</td>
</tr>
<tr>
<td>rtot</td>
<td>Total available amount of RISC protein complexes (# L$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$1.0 \times 10^{15}$</td>
</tr>
<tr>
<td>Ve</td>
<td>Extracellular volume (L)</td>
<td>Specified experimentally in vitro, Estimated from experimental data</td>
<td>$2 \times 10^{-4}$, $1 \times 10^{-5}$</td>
</tr>
<tr>
<td>Vi</td>
<td>Intracellular volume (L)</td>
<td>Literature (47)</td>
<td>$4 \times 10^{-12}$</td>
</tr>
<tr>
<td>Vp</td>
<td>Plasma volume, mouse (L)</td>
<td>Literature (48)</td>
<td>$1.5 \times 10^{-3}$</td>
</tr>
<tr>
<td>kbloodbind</td>
<td>Complex binding to blood components (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$1 \times 10^{-4}$</td>
</tr>
<tr>
<td>kblooddis</td>
<td>Complex dissociation from blood components (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$1 \times 10^{-4}$</td>
</tr>
<tr>
<td>kcleavage</td>
<td>Cleavage of target mRNA by activated RISC complex (h$^{-1}$)</td>
<td>Literature (44)</td>
<td>7.2</td>
</tr>
<tr>
<td>kd egendna</td>
<td>Endosomal siRNA degradation (h$^{-1}$)</td>
<td>Literature (32-34,49)</td>
<td>$5 \times 10^{-1}$</td>
</tr>
<tr>
<td>kd egionna</td>
<td>Intracellular siRNA degradation (h$^{-1}$)</td>
<td>Estimated from experimental data and literature (33)</td>
<td>$2.9 \times 10^{-2}$</td>
</tr>
<tr>
<td>kdegmRNA</td>
<td>Target mRNA degradation (h$^{-1}$)</td>
<td>Literature (50-53)</td>
<td>2</td>
</tr>
<tr>
<td>kdegprot</td>
<td>Target protein degradation, Luciferase (h$^{-1}$)</td>
<td>Literature (25)</td>
<td>$3.5 \times 10^{-1}$</td>
</tr>
<tr>
<td>kdegRISC</td>
<td>Activated RISC complex degradation (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$7.7 \times 10^{-2}$</td>
</tr>
<tr>
<td>kdisRISC</td>
<td>Dissociation of activated RISC complex (h$^{-1}$)</td>
<td>Chosen to be negligible once activated RISC is formed</td>
<td>$1 \times 10^{-5}$</td>
</tr>
<tr>
<td>kdisRISCm</td>
<td>Dissociation of activated RISC complex and target mRNA (h$^{-1}$)</td>
<td>Literature (42-44)</td>
<td>1</td>
</tr>
<tr>
<td>kelimc</td>
<td>Extracellular complex degradation (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$8.7 \times 10^{-2}$</td>
</tr>
<tr>
<td>kelimpl</td>
<td>Plasma complex degradation (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$2.9 \times 10^{-2}$</td>
</tr>
<tr>
<td>kescendna</td>
<td>Endosomal escape for siRNA (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$5.8 \times 10^{-2}$</td>
</tr>
<tr>
<td>kescendvec</td>
<td>Endosomal escape for complex (h$^{-1}$)</td>
<td>Estimated from experimental data and literature (54)</td>
<td>$6 \times 10^{-2}$</td>
</tr>
<tr>
<td>kformmRNA</td>
<td>Formation of target mRNA (# L$^{-1}$ h$^{-1}$)</td>
<td>Estimated from experimental data and literature (54)</td>
<td>$1 \times 10^{-2}$</td>
</tr>
<tr>
<td>kformprot</td>
<td>Formation of target protein (h$^{-1}$)</td>
<td>Literature (50,51)</td>
<td>$5.2 \times 10^{13}$</td>
</tr>
<tr>
<td>kformRISC</td>
<td>Formation of activated RISC protein (L # h$^{-1}$)</td>
<td>Literature (50,51)</td>
<td>$5.2 \times 10^{2}$</td>
</tr>
<tr>
<td>kformRISCm</td>
<td>Formation of activated RISC/mRNA complex(L # h$^{-1}$)</td>
<td>Estimated from experimental data and literature (42-44)</td>
<td>$2 \times 10^{-19}$</td>
</tr>
<tr>
<td>kgrowth</td>
<td>Cell growth rate (h$^{-1}$)</td>
<td>Literature (42-44)</td>
<td>$1.1 \times 10^{14}$</td>
</tr>
<tr>
<td>kint</td>
<td>Internalization (h$^{-1}$)</td>
<td>Determined experimentally</td>
<td>Fit to each system</td>
</tr>
<tr>
<td>ktransblood</td>
<td>Transport from plasma to extracellular fluid (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$1 \times 10^{-2}$</td>
</tr>
<tr>
<td>kunpackcyst</td>
<td>Cytosolic complex unpackaging (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$5 \times 10^{-1}$</td>
</tr>
<tr>
<td>kunpackend</td>
<td>Endosomal complex unpackaging (h$^{-1}$)</td>
<td>Estimated from experimental data</td>
<td>$6 \times 10^{-2}$</td>
</tr>
</tbody>
</table>

For parameters common to both in vitro and in vivo applications, the in vivo parameter values are shown in italics below the in vitro parameter values.

minimal impact on the overall duration (Figure 2A). Using the baseline parameters given in Table 2, the mathematical model predicts the trends observed experimentally (Figure 2B). Similar trends are observed with these siRNA doses in other luciferase-expressing cell lines (data not shown).

**Effect of cell doubling time on luciferase knockdown in vitro**

The majority of studies examining the kinetics of siRNA-mediated gene silencing in vitro have used rapidly dividing cell lines that typically have doubling times of ~1 day. Using these cell lines, the silencing effect generally lasts for ~1 week (27,28). To investigate whether this duration of silencing is intrinsic to siRNA or a result of dilution due to cell division, siRNA-mediated gene silencing was monitored in four luciferase-expressing cell lines with different observed doubling times: Neuro2A-Luc (0.8 days), LNCaP-Luc (1.4 days), HeLa-Luc (1.6 days) and CCD-1074Sk-Luc (nondividing). The cells were plated in 24-well plates and transfected under identical conditions to enable direct observation of the effect of cell doubling time alone. The experimental results in Figure 3A reveal that the dilution effect from cell division can alter the duration of gene silencing. Consistent with previous observations, the duration of gene silencing in rapidly growing cell lines is ~1 week; however, cell lines with slower doubling times show a corresponding increase in the duration of silencing. Figure 3B shows the predicted effect of cell doubling time when the experimental transfection parameters are input into the mathematical model. The model predictions confirm that the dilution effect due to cell doubling time alone can account for the decreased duration of gene silencing in dividing cells. It is interesting to note that the duration of gene silencing in nondividing cells is ~3 weeks. This duration is consistent with the kinetics observed in two previous reports looking at siRNA-mediated gene silencing in nondividing mammalian neurons and primary macrophages (29,30). In nondividing cells, the duration of gene silencing is not controlled by dilution from cell division but by the intrinsic stability of siRNA within the cell.

**Kinetics of luciferase knockdown by siRNA in subcutaneous tumors**

Many tumors exhibit rapid growth with doubling times on the order of only a few days, and the duration of gene silencing

should be limited by this rapid cell division. To test this hypothesis, subcutaneous tumors were created in A/J mice using luciferase-expressing Neuro2A-Luc cells. Since the goal was to observe the kinetics of gene silencing and not an actual therapeutic effect on the growth rate of the cells, siRNA against the luciferase gene (siGL3) and a control siRNA (siCON1) were used to show the sequence-specificity of the luciferase knockdown. Each mouse received three consecutive daily LPTV injections of transferrin-targeted polyplexes containing 2.5 mg/kg siRNA. After quantifying the luciferase activity in each tumor using the Xenogen camera, data were used to create a predicted logistic growth curve (Figure 4A). Because the siRNA targets only the luciferase gene, the growth rate of the cells should be unaffected; as a result, a decrease in luciferase signal intensity indicates a change in the luciferase protein level. Normalization to predicted growth curves allowed estimation of the knockdown resulting from siRNA treatment (Figure 4B).

By adjusting only the parameters for the circulation/extracellular transport of the siRNA polyplexes, very good agreement was obtained between the model’s predictions and the experimental data. The observed knockdown duration after three consecutive injections was around 10 days, consistent with the in vitro data for cell lines with similar observed growth rates.

Kinetics of luciferase knockdown by siRNA in hepatocytes

While cells in subcutaneous tumors are dividing rapidly (e.g. once per day), most of the hepatocytes in a normal mouse liver are in a state of growth arrest (31). Therefore, it was hypothesized that gene silencing by siRNA would exhibit different kinetics in hepatocytes versus tumors. Each BALB/c mouse received a single HPTV injection of 0.25 mg/kg plasmid and...
acids are rapidly degraded in serum, current efforts in the field of nucleic acid-based therapeutics seek to enhance the stability of the nucleic acids with the goal of increasing the duration of gene silencing by boosting their bioavailability and possibly prolonging their persistence intracellularly (32–34). Layzer and co-workers studied the kinetics of gene silencing in HeLa cells using 2'-F-modified siRNA and unmodified 2'-OH siRNA. Although the 2'-F-modified siRNA led to a significant increase in serum stability, it appeared to have no effect on the duration of gene silencing after transfection. This suggests that the intracellular stability of siRNA molecules is not the limiting factor controlling the duration of gene silencing in rapidly dividing cells; instead, dilution due to cell division limits how long gene silencing can occur under these conditions. If the intracellular half-life of siRNA molecules is not the limiting factor controlling the duration of gene silencing in rapidly dividing cells; instead, dilution due to cell division limits how long gene silencing can occur under these conditions. If the intracellular half-life of siRNA molecules is not the limiting factor controlling the duration of gene silencing, it will be shorter than the cell doubling time, meaning dilution due to cell division will no longer be the dominant factor. Increasing the persistence of siRNA within the cell will prolong the duration of gene silencing. Results from such studies in nondividing cells should be interpreted carefully since the apparent intracellular stability of

2.5 mg/kg siGL3 on day 0, and the Xenogen camera was used to follow the luciferase signal in each mouse liver. Normalization to the signal intensity in mice that received plasmid only (no siRNA) allowed quantification of the percent knockdown by siRNA. Figure 5 shows the experimental data together with the model predictions. Similar to the in vitro results for gene silencing in nondividing cells, the duration of gene silencing lasts for ~3–4 weeks in the hepatocytes after a single dose of siRNA.

**Effect of siRNA stability on luciferase knockdown by siRNA**

Because both double-stranded and single-stranded nucleic acids are rapidly degraded in serum, current efforts in the

Figure 4. Kinetics of luciferase knockdown by siRNA in Neuro2A-Luc subcutaneous tumors in A/J mice. (A) Experimental and predicted results for luciferase knockdown after three consecutive LPTV injections on days 6, 7 and 8 of transferrin-targeted CDP-im polyplexes containing 50 µg siRNA per 20 g mouse. Experimental data points are shown for a mouse receiving siCON1 (squares) and a mouse receiving siGL3 (circles). Solid lines represent the predicted luciferase signal with siRNA treatment and dashed lines represent the predicted luciferase signal in the absence of siRNA treatment. (B) Normalization of the observed luciferase signal in the siGL3-treated mouse to the predicted luciferase signal in the absence of treatment. Circles indicate the normalized experimental data points, while the solid line represents the response predicted by the mathematical model using the baseline *in vivo* parameters given in Table 2 and assuming that 50% of the total cells are reached with each dose.

Figure 5. Kinetics of luciferase knockdown by siRNA in nondoning hepatocytes in BALB/c mice. Experimental and predicted results are shown for luciferase knockdown after hydrodynamic tail-vein co-injection of 5 µg pApoEHCRLuc and 50 µg siRNA per 20 g mouse on day 0. Circles represent the ratio of the average luciferase signal intensity from three mice receiving plasmid + siRNA to the luciferase signal intensity from three mice receiving plasmid alone. The predicted luciferase knockdown, given by the solid line, was calculated using the baseline *in vivo* parameters given in Table 2 with the following modifications to account for hydrodynamic injection of naked siRNA without a delivery vehicle: eliminate steps involving the complexes (kendna, kdepndna, ktransblood), modify uptake and intracellular trafficking to match observed kinetics (partition = 1 × 10^-2, ktransblood = 1, kint = 1 × 10^-3 h^-1, ksedn = 5 × 10^-3 h^-1), and modify extracellular volume (Ve = 1.5 × 10^-5 L). The ksendna and ksedn may no longer represent endosomal processes as hydrodynamically injected naked siRNA may be internalized through different vesicles or partitioned into a separate intracellular compartment (e.g. nucleus) that exhibits different degradation and release kinetics than in standard or receptor-mediated endocytosis of siRNA-containing complexes. The total number of hepatocytes was chosen to be 5 × 10^7, on the same order of magnitude as the number of hepatocytes in a mouse liver (40,41).
siRNA molecules may be caused by association with other intracellular components or localization to specific compartments, both of which could lead to degradation kinetics independent of the properties of the siRNA molecules alone. In that case, modified siRNA would not necessarily increase the duration of gene silencing relative to unmodified siRNA even in nondividing cells.

Multiple doses to prolong luciferase knockdown by siRNA in nondividing cells

The previous studies have looked at the transient knockdown of the luciferase reporter gene by 1–3 injections of siRNA over a short-term period; even in nondividing cells, the maximum duration of silencing using typical siRNA doses is ~3–4 weeks. However, a clinically relevant treatment regimen using siRNA may require that a gene be silenced for a prolonged period of time. Some have attempted to solve this problem by using lentiviral delivery of expressed short-hairpin siRNAs (shRNAs) to achieve sustained gene silencing in vitro and in vivo (35,36). Precise control of the intracellular level of siRNA and having a means to turn off its production when treatment is no longer necessary represent two major challenges to this use of shRNA. On the other hand, the intrinsically transient nature of siRNAs makes them more amenable to disease treatments in which the treatment is given over a period of time and then stopped once the desired therapeutic outcome (e.g. regression of a tumor or inhibition of viral growth) is achieved. To illustrate how properly timed doses of siRNA can prolong gene silencing by siRNA, nondividing CCD-1074Sk-Luc cells were transfected with a second dose of siRNA 4 days after the initial dose (Figure 7A). With a second dose of 100 nM siRNA, the luciferase protein levels remained at <40% of the steady-state value for an additional 4 days. If the trends continue in such a fashion, a 100 nM dose every 4 days could lead to persistent gene silencing as shown by model calculations in Figure 7B.

Considerations for siRNA-based treatments that require a threshold knockdown for efficacy

Because siRNA treatment of rapidly dividing cells requires treating more cells over time while also having to deal with dilution effects, the amount of target gene or protein knockdown will be less than that observed in slowly dividing or nondividing cells. More frequent dosing is required to overcome these barriers. Cancer is one example of a disease often characterized by rapid cell division that may require target gene knockdown lasting longer than that which can be achieved with a single dose of siRNA. To address this situation, the mathematical model was used to estimate siRNA dosing schedules needed to maintain a given gene below a
threshold value for an extended period of time in dividing cells. While the magnitude of target gene (or protein) reduction or the duration of knockdown relative to the steady-state value in the absence of treatment can be relatively good indicators of the success of an siRNA treatment, the therapeutic efficacy of an siRNA treatment regimen should perhaps be judged by the length of time it is able to maintain the target gene or protein level below a given threshold. Although a short, substantial knockdown of certain targets may be sufficient to trigger a cascade of downstream effects, other situations may require considerably longer knockdown to achieve the desired therapeutic effect. Additionally, this therapeutic effect may only be seen when the target protein is reduced below a threshold, or some fraction of its pre-treatment value.

The data in Figure 8 show how the mathematical model can be used to simulate the effects of cell doubling time and target protein half-life during treatment with siRNA. To avoid unnecessary complications, the calculations ignore the circulation/extracellular transport and consider each siRNA dose already in the local extracellular environment of the cells (analogous to the \textit{in vitro} situation). Figure 8A–D gives results that demonstrate how target protein half-life can impact the observed dynamics of protein knockdown with once- or twice-weekly dosing in rapidly dividing or nondividing cells. For a target protein with a short half-life in rapidly dividing cells, once-weekly dosing is adequate to maintain persistent knockdown of the target protein half-life; then, knockdown of the target mRNA may not result in protein knockdown if the target protein half-life is very long (Figure 8D). The fraction of the total treatment time during which a target protein is below a threshold (e.g. 50% steady-state value) can be used as a metric to compare the efficacy of different treatment regimens. The data illustrated in Figure 8E reveal how cell growth rate and target protein half-life can affect protein knockdown when siRNA is administered once on day 0, once-weekly or twice-weekly over the 25-day treatment. As expected, cell growth rate has a large impact on the duration of knockdown, directly affecting the fraction of the total time that the target protein level can be reduced below the threshold of 50%.

**DISCUSSION**

A more thorough understanding of the factors affecting the kinetics of siRNA-mediated gene silencing should prove to be invaluable for experimental and clinical applications of siRNA. Given the relatively recent discovery of RNAi, details of its action are still being elucidated, and many of the current siRNA dosing schedules used in literature are based on precedence rather than being optimized for each system. The high cost of siRNA molecules, especially for \textit{in vivo} studies, limits systematic exploration of the parameter space needed to achieve the most effective siRNA dosing schedule for each model system. This situation can be partially rectified by using mathematical modeling to give insights that help direct experimental studies. Here, we employed bioluminescent imaging and mathematical modeling to investigate the effects of target-specific and treatment-specific parameters on siRNA-mediated gene silencing \textit{in vitro} and \textit{in vivo}.

The experimental data presented here show the effects of cell doubling time, siRNA dosing schedule, and siRNA delivery method on luciferase reporter-protein knockdown and aid in developing mathematical models of siRNA delivery to and function within mammalian cells. Luciferase knockdown in cell lines engineered to constitutively express luciferase was used to mimic the knockdown of an endogenously expressed gene, analogous to an oncogene whose presence in a cell can lead to tumorigenicity. The luciferase-expressing cell lines were used in cell culture experiments or injected into mice and then monitored for luciferase expression using noninvasive bioluminescent imaging with the Xenogen Imaging System. The duration of gene silencing lasted for \~1 week in rapidly dividing cells but longer than 3 weeks in nondividing cells both \textit{in vitro} and \textit{in vivo}, supporting the hypothesis that dilution due to cell division is the major factor controlling the duration of luciferase knockdown in rapidly dividing cells.

The duration of gene silencing by siRNA can be longer than that achieved with other nucleic acid-based gene inhibition strategies, such as antisense, whose knockdown typically lasts only on the order of 1–2 days. Bertrand and co-workers (37) studied antisense- and siRNA-mediated inhibition of GFP in HeLa cells and showed that antisense-mediated inhibition diminished after only 1 day, the siRNA-mediated inhibition was still increasing. This significant difference in the duration of gene silencing could become important when trying to use either antisense or siRNA molecules as therapeutic agents. In fact, the short duration of gene silencing by certain nucleic acid-based gene inhibition strategies could preclude their ability to alter cellular behavior if the target gene is not silenced for an adequate amount of time. This would be particularly apparent if the target protein has a long intracellular half-life; then, knockdown of the target mRNA may not result in target protein knockdown if the mRNA levels can be restored before a significant amount of protein has degraded.

The findings presented here highlight several key considerations for experimental design when evaluating the efficacy of siRNA against certain genes that produce proteins with long half-lives. If the knockdown phenotype does not become apparent until the protein is below a certain threshold, then observation at early time points may not reveal any effect. This is crucial for \textit{in vitro} studies aimed at testing the ability of a therapeutic siRNA to induce apoptosis or growth arrest in certain cell lines. Common practice is to look at time points within 48 and 72 h; here, model predictions suggest that these time points may be too early if the target protein half-life is any longer than a couple of days. Similar considerations should be made when deciding dosing schedules for \textit{in vivo} studies using siRNA for protein knockdown in tumors (e.g. an oncogenic fusion protein), since proteins with longer half-lives will show a slower initial response to the therapy but will require less frequent dosing for persistent silencing. An important area for future research will be to determine to what extent a gene or protein needs to be knocked down before the intended therapeutic effect is realized. Such information can be combined with mathematical models like the one presented here to more...
Figure 8. Effect of cell doubling time and target protein half-life on the ability to maintain persistent gene silencing. All plots represent predicted mRNA (dashed lines) and protein (solid lines) knockdown in transfected cells using the baseline in vitro parameters given in Table 2, a transfection time of 5 h, and an initial number of dividing and nondividing cells equal to $5 \times 10^4$ and $1.5 \times 10^5$, respectively. (A) Dose of 100 nM siRNA every 3 days with a target protein half-life of 2 h ($k_{\text{degprot}} = 0.35 \text{ h}^{-1}$) in cells with a doubling time of 1 day ($k_{\text{growth}} = 0.029 \text{ h}^{-1}$). (B) Dose of 100 nM siRNA every 3 days with a target protein half-life of 48 h ($k_{\text{degprot}} = 0.014 \text{ h}^{-1}$) in cells with a doubling time of 1 day ($k_{\text{growth}} = 0.029 \text{ h}^{-1}$). (C) Dose of 100 nM siRNA every 7 days with a target protein half-life of 2 h ($k_{\text{degprot}} = 0.35 \text{ h}^{-1}$) in nondividing cells. (D) Dose of 100 nM siRNA every 7 days with a target protein half-life of 48 h ($k_{\text{degprot}} = 0.014 \text{ h}^{-1}$) in nondividing cells. (E) Effect of variations in cell doubling time and target protein half-life on the ability to maintain a target protein level below a threshold of 50% its pre-treatment value over the 25-day period. I, 100 nM (day 0); II, 100 nM (days 0, 7, 14); III, 100 nM (days 0, 3, 7, 10, 14, 17, 21, 24). Surface vertices represent the fraction of the total time during which the relative protein level is below the 50% threshold.
accurately determine the required treatment regimen needed to achieve efficacy. Although the model in its current form does not allow for treatment effects other than target gene knockdown, the simple addition of a death parameter to the cell growth equation could provide a target cell death rate that depends on the reduction of the target protein level below a certain threshold. Other slightly more complicated modifications to the current set of equations could incorporate recruitment of immune effector cells, effects on angiogenesis or even sensitization to other treatments including chemotherapy.

While the mathematical model can predict many of the trends observed experimentally for the systems used here, confidence in the actual magnitude and duration of the predicted gene silencing in hypothetical situations can still be greatly increased as more accurate parameter values become available. Parametric sensitivity analysis was performed using the SENS_SYS modification of the ODE15s solver in MATLAB. Parameters governing RISC formation ($k_{\text{formRISC}}$ and binding to target mRNA ($k_{\text{formRISCm}}$) have a significant impact on target mRNA or protein levels. Although studies of the RISC complex are rapidly elucidating details of its mechanism and kinetics, these parameters will need to be refined as more data become available. Additional equations will be needed to model a multi-step RISC formation process, or the lumped rate constants currently used can be modified to provide reasonable estimates of the overall kinetics. As expected, target mRNA and protein levels are also sensitive to parameters governing the siRNA delivery process, such as cellular uptake, endosomal escape and vector unpackaging. It will be important to determine these parameters for each individual delivery vehicle since such rates will vary from system to system. With knowledge of these different parameters, the model can be used to mimic delivery by a variety of methods including naked siRNA (by high-pressure or low-pressure tail-vein injection) or formulation into liposomes, lipoplexes or polyplexes. Such comparisons may reveal how the characteristics of each delivery method specifically affect the kinetics of gene silencing. This information may help to focus design improvements for delivery vehicles or improve the efficacy of treatment regimens employing them, as suggested in general for gene delivery by Varga and co-workers (38). Of the parameters intrinsic to the target cells, the most important are the cell growth rate (dilution effect), compartment volumes (that control the concentration of siRNA available to drive uptake or association processes), and the stability of the target mRNA and protein molecules. The current set of model equations predicts that the stability of the mRNA transcript has a greater effect on the magnitude and duration of gene silencing than the absolute transcript number. This is because the relative knockdown is controlled largely by the relative sizes of the two mRNA degradation terms: natural turnover within the cell and degradation by RNAi. Therefore, the contribution from RNAi leads to greater deviation from the steady-state mRNA level for more stable mRNA molecules. Similar reasoning can be applied to other gene inhibition strategies, such as antisense, that act at the mRNA level (39).

Based on these findings and the literature to date, siRNA appears to be the most potent and effective nucleic acid-based therapeutic aimed at post-transcriptional gene silencing. The siRNA molecules can achieve $>$80% target protein inhibition at nanomolar concentrations, and their enhanced intracellular stability enables knockdown that can last for weeks in nondividing cells. It is shown here that an optimized siRNA-based treatment schedule can be designed to achieve prolonged gene silencing by properly timed injections of siRNA. Mathematical modeling can help to realize these optimized treatments at a fraction of the time and cost that would be required by experimentation alone. Although there is no substitute for experimental data, especially for highly variable and not completely definable biological systems, model calculations can help to guide effective experimental design and aid in data interpretation. With the burgeoning interest in nucleic acid-based therapeutics such as siRNA, development of mathematical models such as the one presented here may expedite their translation into clinically relevant therapeutics for disease treatment and management.

**SUPPLEMENTARY DATA**

Supplementary Data are available at NAR Online.

**ACKNOWLEDGEMENTS**

The authors are especially grateful to D. Petersen and D. Kohn (Children’s Hospital Los Angeles) for performing the lentiviral transductions of the luciferase-expressing cell lines; A. McCaffrey and M. Kay (Stanford University) for donating the luciferase-containing plasmid; and J. Heidel (Calando Pharmaceuticals, Inc.) for performing bioluminescent imaging of the mice used in the HPTV studies looking at hepatocyte-specific luciferase expression. This material is based upon work supported under a National Science Foundation Graduate Research Fellowship. This publication was made possible by Grant Number 1 R01 EB004657-01 from the National Institutes of Health (NIH). Its contents are solely the responsibility of the authors and do not necessarily represent the official views of the NIH. Funding to pay the Open Access publication charges for this article was provided by the California Institute of Technology.

**Conflict of interest statement.** None declared.

**REFERENCES**


